



# The Dark Side and its Nature

Madrid, June 20, 2006  
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## The density quest in the 90's

$$q_0 \sim 0$$

$$\Omega_m = 0.2-0.3$$

0CDM

or  
vs

$$\Omega_m \sim 1 ?$$

SCDM

$$q_0 \sim 0.5$$

Supported by apparent  
slow evolution

Supported by CMB  
(COBE) data

Inflationary models  
can make it acceptable  
without fine tuning

Generic inflationary  
prediction

SN Ia as standard candles gave an  
unexpected reply

$$q_0 \sim -0.6-0.7$$

$$\Omega_m = 0.2-0.3$$

&

$$\Omega_o \sim 1$$

the gap is covered by Dark Energy

Riess  
et al, 1998,  
AJ116, Perlmutter  
et al, 1999,  
ApJ 517

SN Ia

cosmic expansion is  
accelerated

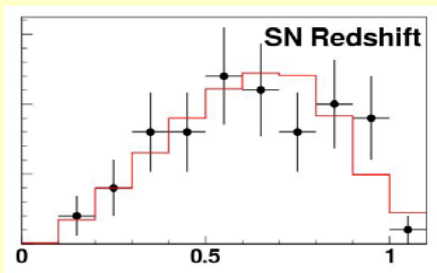
SNLS: *Astier et al (2005) A&A*

Only acceptable model with  
sound historical records

LCDM

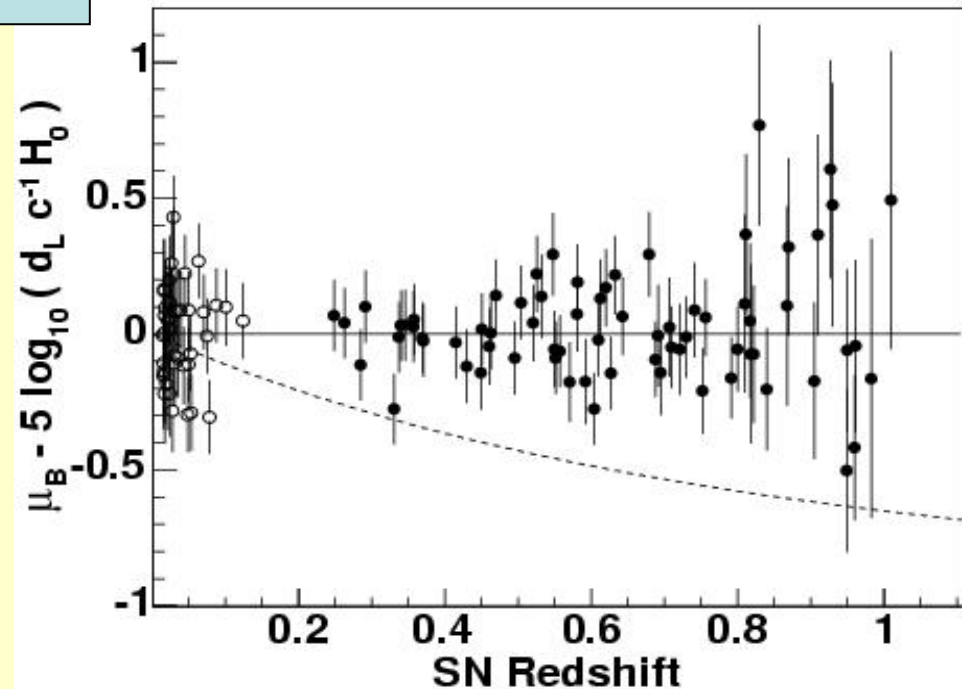
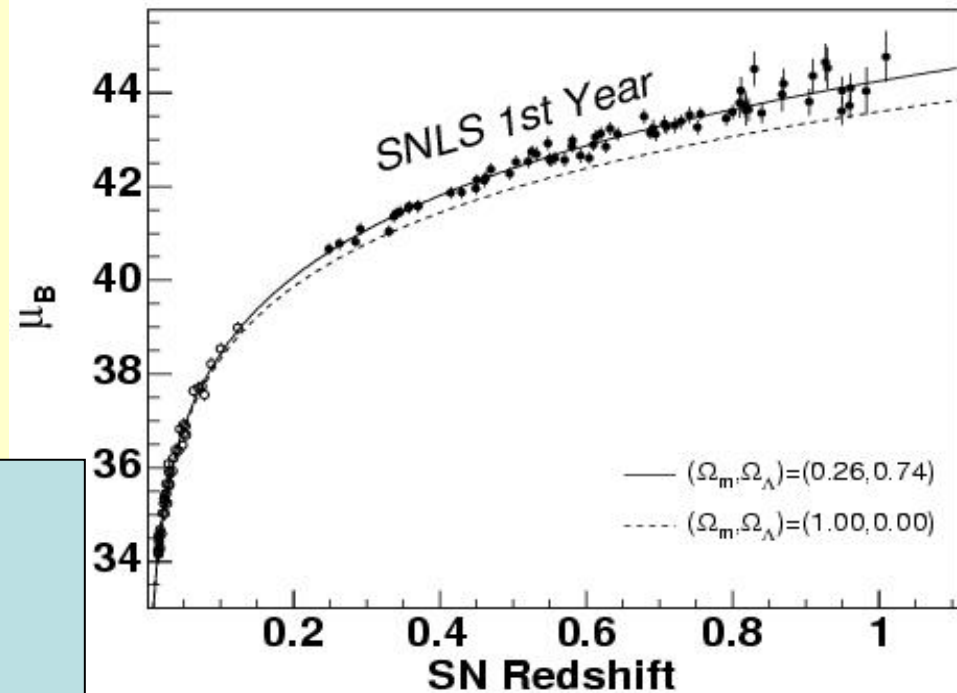
$$d_L H/c \cong z + z^2(1-q)/2 + \dots$$

$$q = \Omega_m/2 - \Omega_\Lambda$$

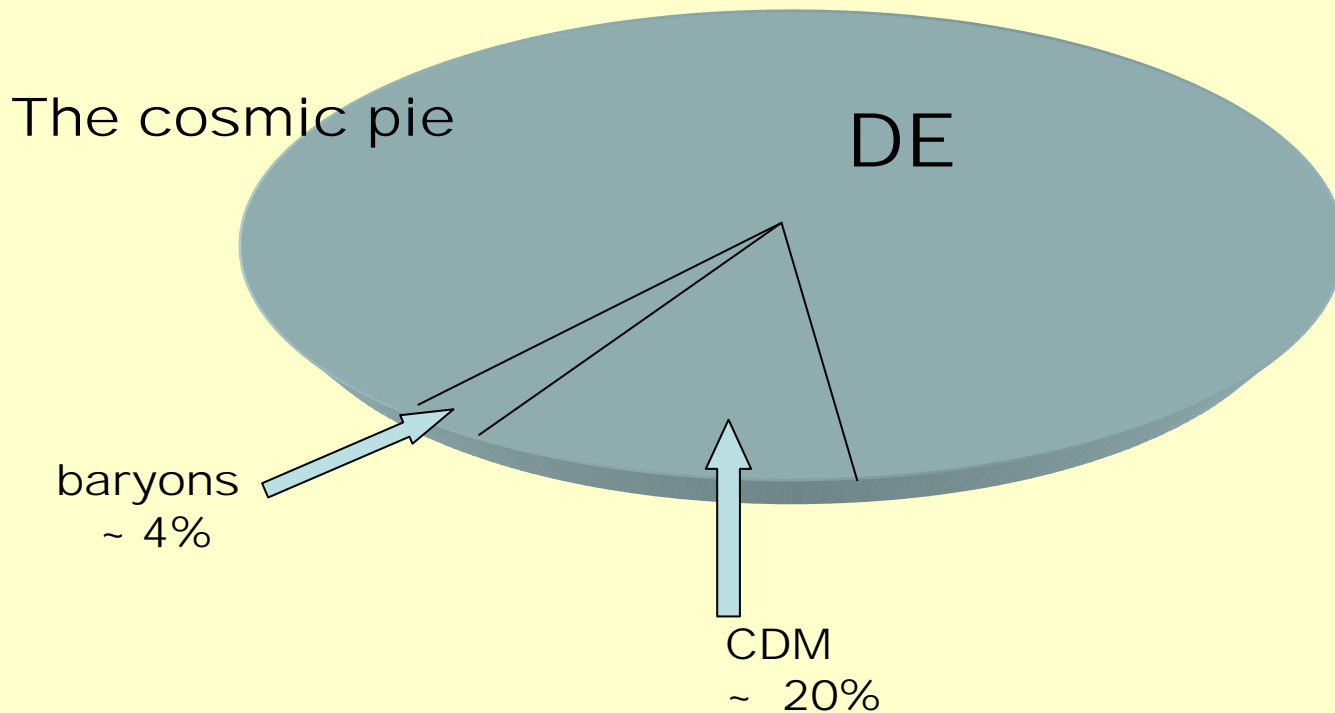


$$\Omega_m = 0.26$$

$$\Omega_{de} = 0.74$$



- DE, what is that ?
- Dont' worry, its' just cosmological constant

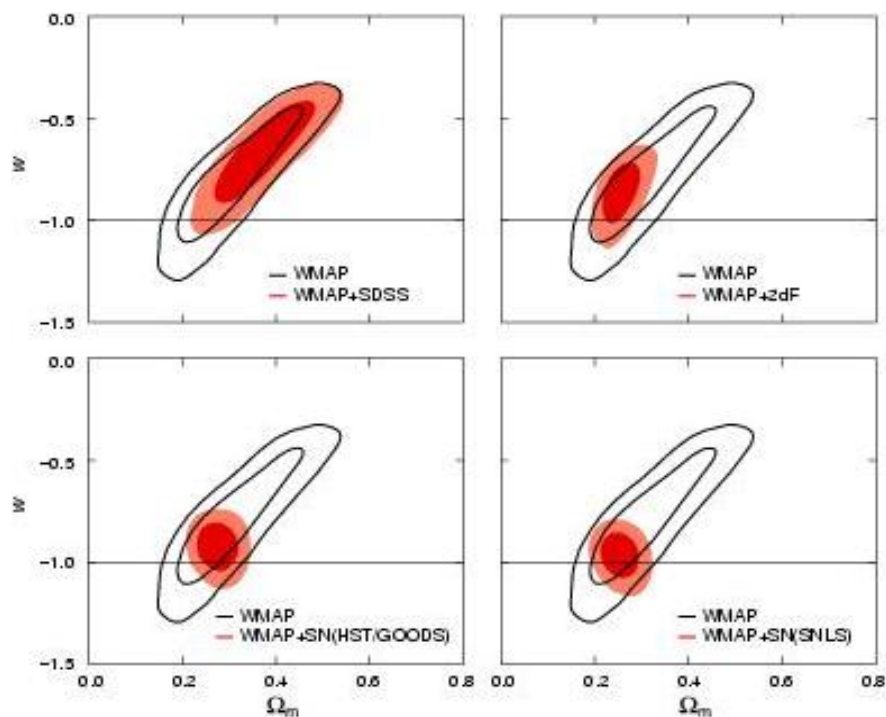


- Fire, fire !
- Dont' worry, its' just incandescent plasma

Table 5:  $\Lambda$ CDM Model: Joint Likelihoods


<i>Parameter</i>	<i>WMAP Only</i>	<i>WMAP +CBI +VSA</i>	<i>WMAP + ACBAR +BOOMERanG</i>	<i>WMAP+ 2dFGRS</i>
$\Omega_b h^2 (\times 10^2)$	$2.233^{+0.072}_{-0.091}$	$2.212^{+0.066}_{-0.084}$	$2.231^{+0.070}_{-0.088}$	$2.223^{+0.066}_{-0.083}$
$\Omega_m h^2$	$0.1268^{+0.0072}_{-0.0095}$	$0.1233^{+0.0070}_{-0.0086}$	$0.1259^{+0.0077}_{-0.0095}$	$0.1262^{+0.0045}_{-0.0062}$
$h$	$0.734^{+0.028}_{-0.038}$	$0.743^{+0.027}_{-0.037}$	$0.739^{+0.028}_{-0.038}$	$0.732^{+0.018}_{-0.025}$

WMAP2+  
parameter  
values



WMAP2+  
contours on  
the  $w$ - $\Omega_m$   
plane

The most immediate candidate: VACUUM ENERGY  
however .....

as  $\rho_o \approx (10 T_o)^4$  and  $\rho_{vac,EW} \approx T_{EW}^4$   
CMB temp. 

$$10 T_o : T_{EW} \sim 1 : 10^{14}$$

$$\rho_\Lambda : \rho_{EW} \sim 1 : 10^{56}$$

horrible  
fine  
tuning

But, recall that  $T_{EW} : T_{GUT} \sim 1 : 10^{14}$

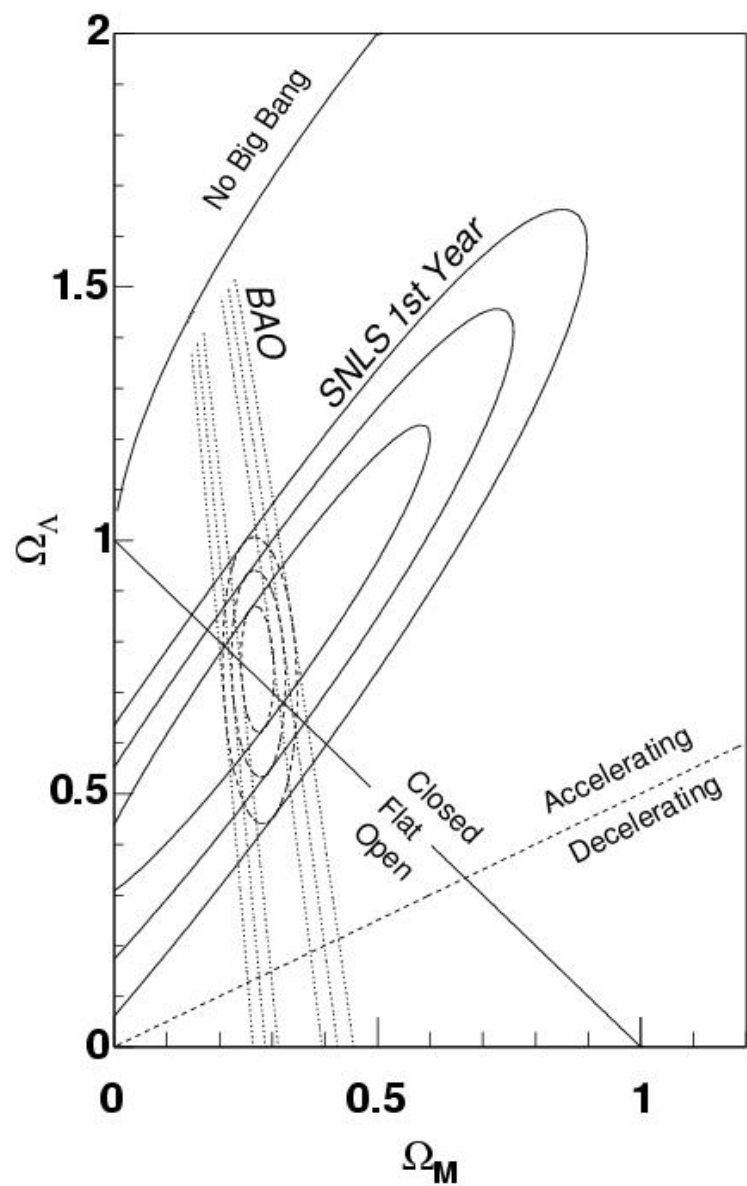
A recent and still unfinished phase transition ?  
perhaps concerning the neutrino sector ....

Frieman et al, 1995 P.R.L. 75

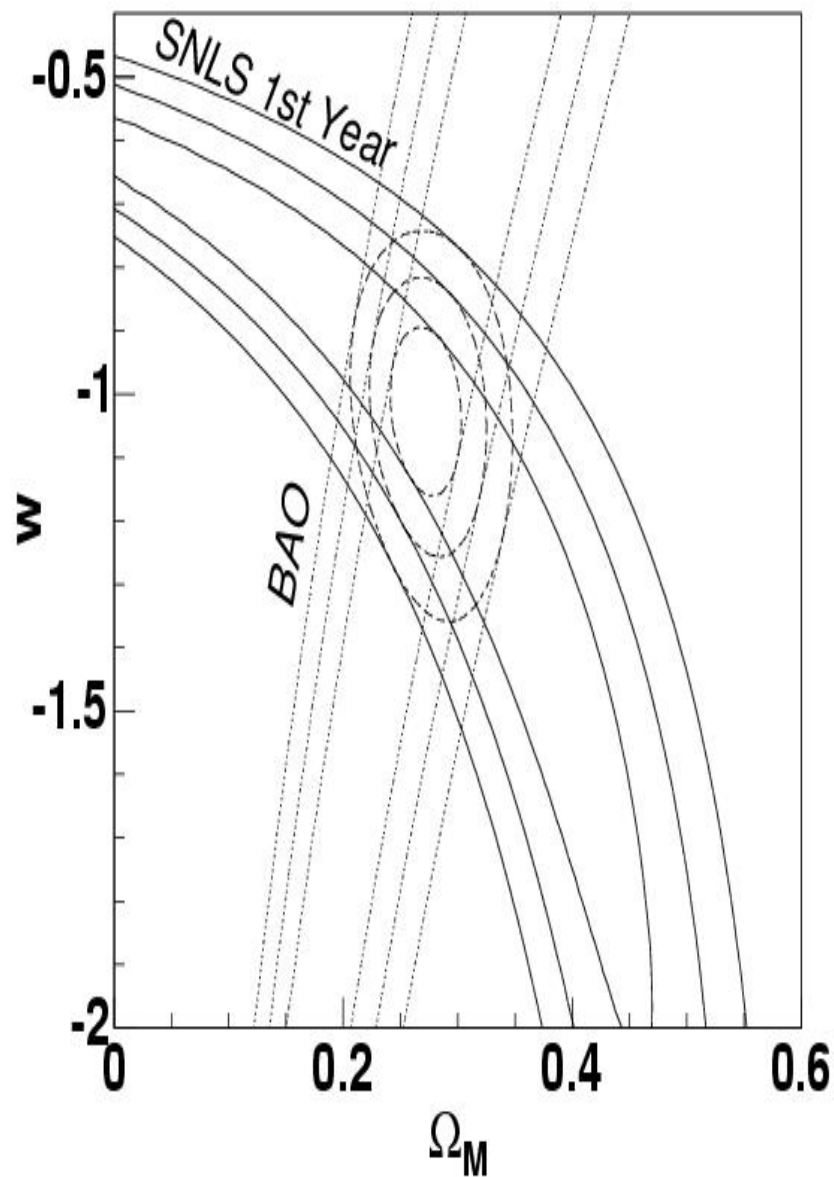
Weiss, 1987 P.L. B 42

Amendola & Barbieri CERN-PH-TH/2005-163

Matter-DE constraints



pressure/density ratio



Otherwise

DE is a scalar field

$$\rho = \dot{\phi}^2 / 2 + V(\phi)$$

$$p = \dot{\phi}^2 / 2 - V(\phi)$$

$$w = p / \rho \sim -1$$

if  $V(\phi) \gg \dot{\phi}^2$ , potential energy  $\gg$  kinetic energy

This depends on the choice of  $V(\phi)$   
& of "initial conditions" on  $\phi'$  and  $\phi''$

dDE apparently eliminates fine-tuning

$$V(\phi) = \Lambda^{\alpha+4} / \phi^\alpha \quad \text{RP potential}$$

$$V(\phi) = (\Lambda^{\alpha+4} / \phi^\alpha) \exp[4\pi(\phi / m_P)^2] \quad \text{SUGRA potent.}$$

fine tuning hidden in  
why we use "field" representation  
instead of N (number of particles) representation  
N is diagonal  $\rightarrow$  w positive

dDE: Wetterich, 1988, N.P.B302  
Ratra&Peebles, 1988, P.R.D37

Tracking  
potentials preferred,  
so getting rid of I.C.  
dependence

Scale  $\Lambda$   
in the energy range of EW transition  
or SUSY break

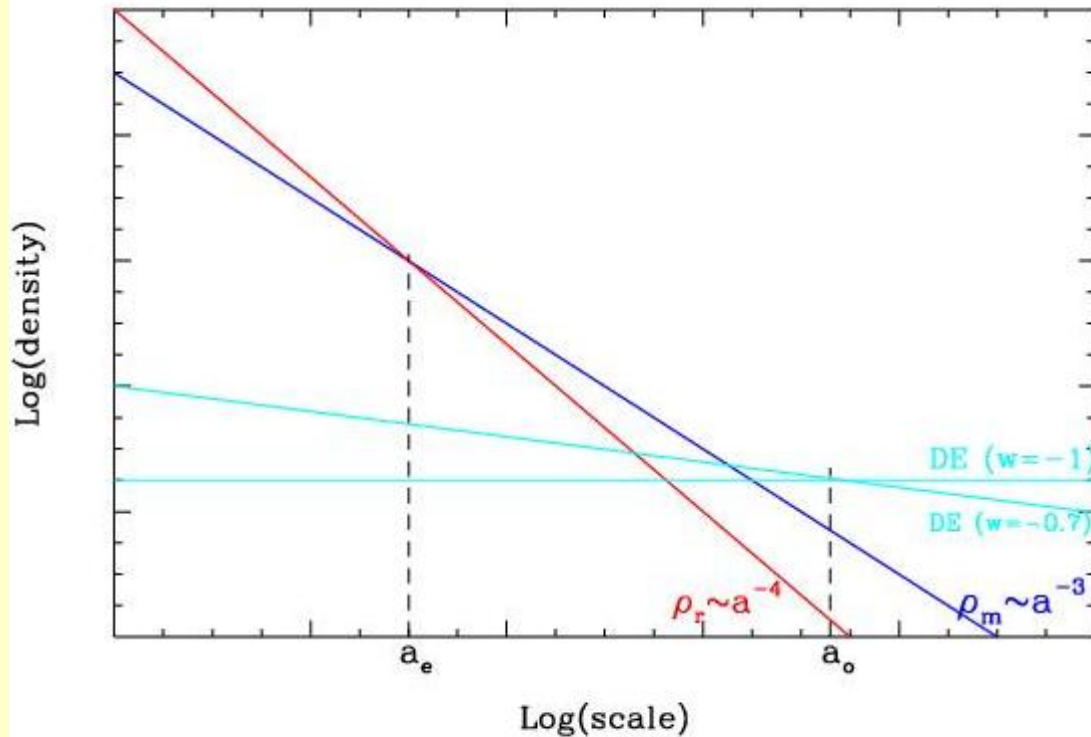
Brax&Martin, 1999, P.L.B468  
and 2001, P.R.D62  
+Riazuelo, 2000, P.R.D61



Dynamical Dark Energy may ease the fine tuning problem, but it does not eliminate

The coincidence problem

DE emerges, as significant cosmic component, just at the eve of our epoch



A possible  
way out:  
DE & DM  
coupled

Say it otherwise:  
The Dark Substance has  
a complex eq of state:  
partially it clusters (DM)  
partially it doesn't (DE)...

... and we try to approach  
phenomenologically such substance  
using DM-DE coupl.

$$ds^2 = a^2(\tau)(-d\tau^2 + dx_i dx^i), \quad (i = 1, \dots, 3)$$

conformal time

$$\ddot{\phi} + 2\frac{\dot{a}}{a}\dot{\phi} + a^2\frac{\partial V}{\partial\phi} = \frac{4}{m_p^2}\sqrt{\frac{\pi}{3}}\beta a^2\rho_c$$

Coupling intensity set by  $\beta$  value

$$\dot{\rho}_c + 3(\dot{a}/a)\rho_c = -\frac{4}{m_p^2}\sqrt{\frac{\pi}{3}}\beta\rho_c\dot{\phi}$$

Energy flow from DM to DE

Wetterich, 1995, A&A 301; Amendola, 1999, P.R.D60; Bartolo & Pietroni, 2000, P.R.D61; Bean & Magueijo, 2001, P.L.B 517; Gasperini, Piazza & Veneziano, 2002,, P.R.D65; Comelli, Pietroni & Riotto, 2003, P.L.B571; etc.

$$\theta_{c,b} = i\frac{\mathbf{k} \cdot \mathbf{v}_{c,b}}{\mathcal{H}}, \quad \mathcal{H} = \dot{a}/a, \quad \mathbf{k}: \text{wavenumber}$$

$$': \text{differentiation with respect to } \alpha = \ln a, \quad X = \sqrt{4\pi/3}\dot{\phi}/(m_p\mathcal{H})$$

$$\delta_c'' = -\delta_c'(1 + \frac{\mathcal{H}'}{\mathcal{H}} - 2\beta X) + \frac{3}{2}(1 + \frac{4}{3}\beta^2)\Omega_c\delta_c + \frac{3}{2}\Omega_b\delta_b$$

$$\delta_b'' = -\delta_b'(1 + \frac{\mathcal{H}'}{\mathcal{H}}) + \frac{3}{2}(\Omega_c\delta_c + \Omega_b\delta_b)$$

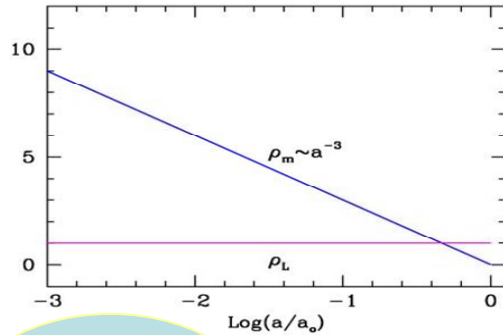
$$\theta_c' = -\theta_c(1 + \frac{\mathcal{H}'}{\mathcal{H}} - 2\beta X) - \frac{3}{2}(1 + \frac{4}{3}\beta^2)\Omega_c\delta_c - \frac{3}{2}\Omega_b\delta_b,$$

$$\theta_b' = -\theta_b(1 + \frac{\mathcal{H}'}{\mathcal{H}}) - \frac{3}{2}(\Omega_c\delta_c + \Omega_b\delta_b).$$

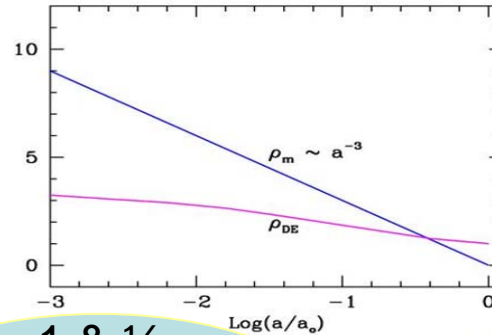
eqs. for  
fluctuation  
evolution

+ usual ones for baryon  
& radiative components

# From LCDM to dDE & cDE

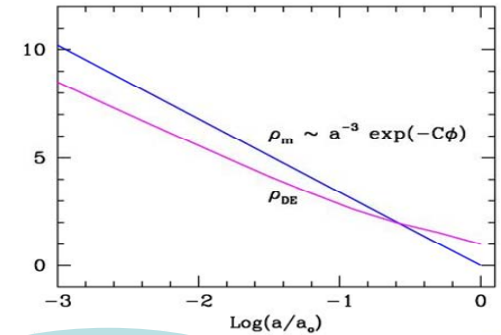


2 problems:  
fine tuning,  
coincidence



1 & ½  
problems: fine tuning  
eased; coincidence  
remains

cost:  $\Lambda$  par. in DE pot.



fine tuning  
& coincidence:  
both eased

cost:  $\Lambda$  par. in DE pot.  
+ coupling par.  $C$

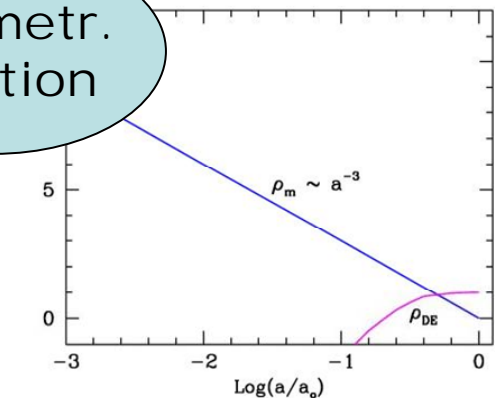
An alternative view (Kolb, Riotto, Matarrese, ... 2005  
see also Buckert 1980, Ellis 1990 ...)

$$g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}$$

standard  $\eta_{\mu\nu}$  defined by  $a(\tau)$  &  $\kappa$  coming from ass.  
state eqs. ( $p=w\rho$ );  $h_{\mu\nu}$  initially linear,  
then developing non-linearities

new  $h_{\mu\nu}$  initially linear  
when extreme non-linearities developped  
backg.state eqn modified

Geometr.  
solution



$\rho_{dE}$  growth together with heavy non-linearities

# Coupling compatible with data ?

Seeking  
limits on  $\beta$

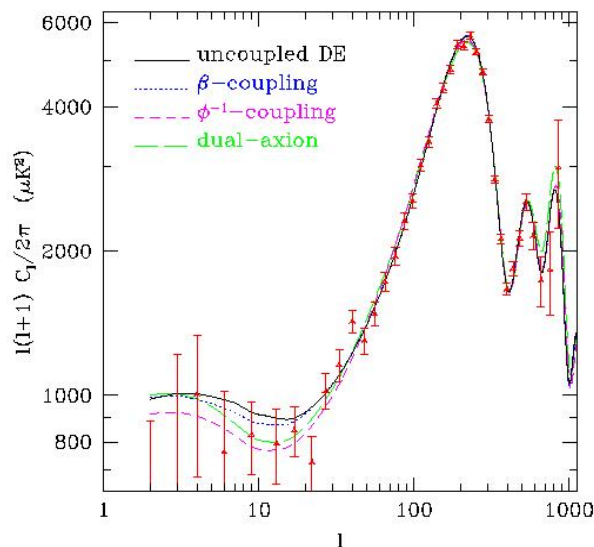
e.g., baryons could not be coupled to DE, this would cause unacceptable changes in their effective gravity

## CMB data

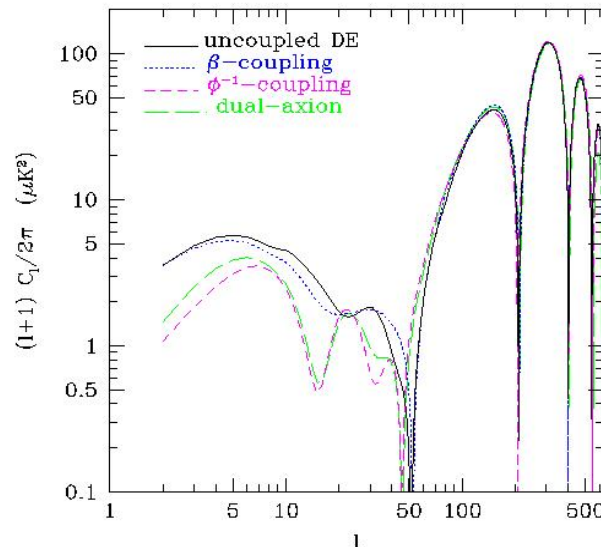
	$\chi^2$	probability	
$\Lambda$ CDM	1.066	4.7 %	
dDE	1.064	5.0 %	(SUGRA)
$\beta$ -coupling	1.066	4.7 %	(SUGRA)
$\phi^{-1}$ -coupl.	1.074	2.9 %	(SUGRA)

from  
Colombo, Mainini & B.,  
2005, ApJ632  
WMAP1 data

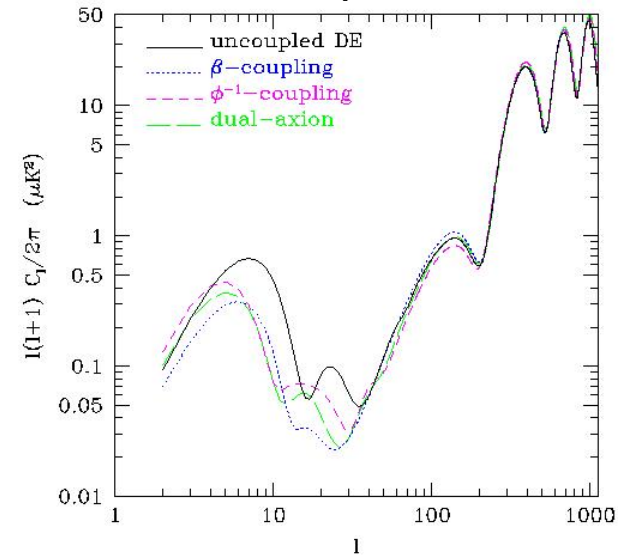
## anisotropy spectrum



## T-E correlation spectrum

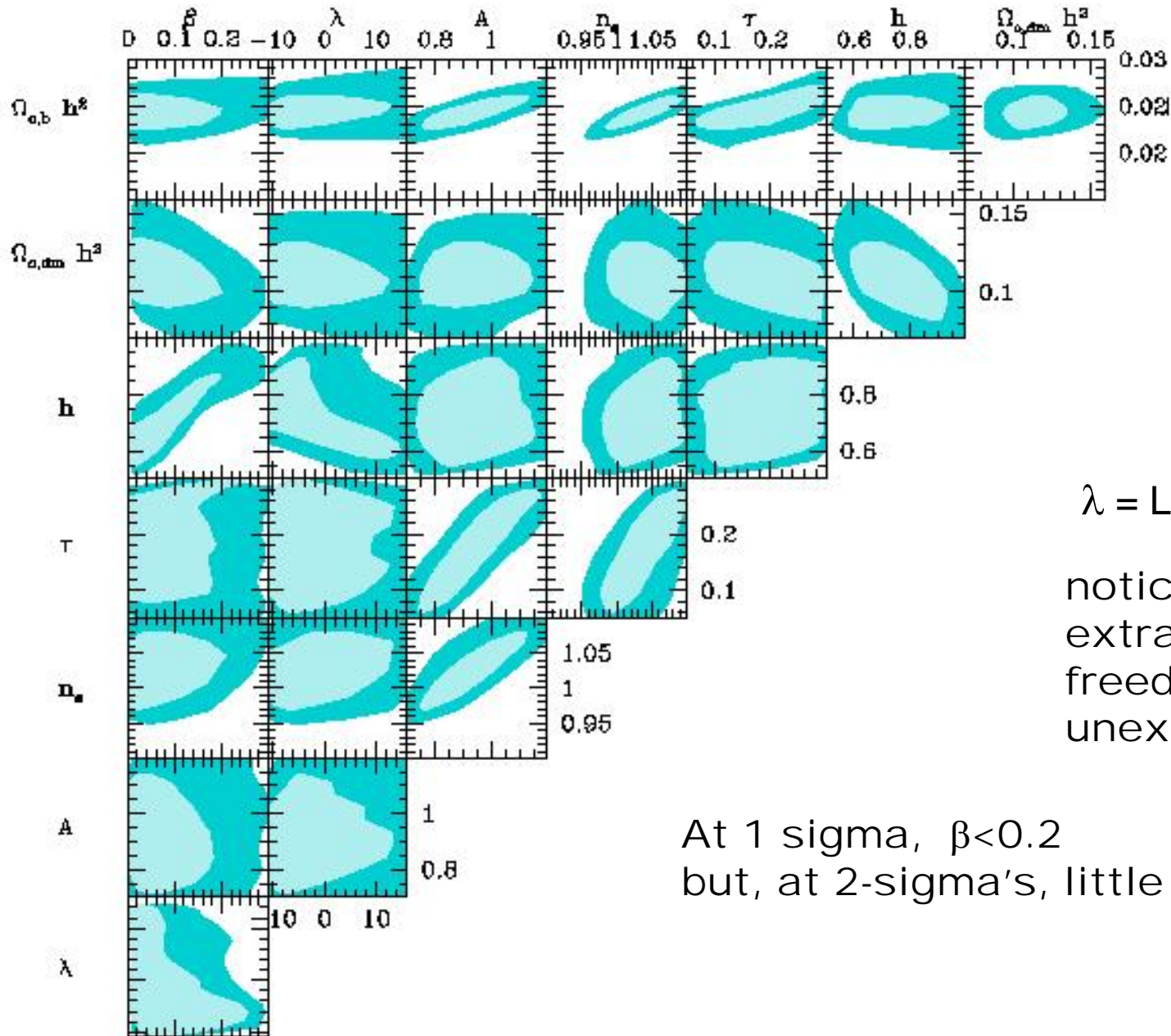


## E-mode spectrum



# Cosmological parameters for cDE with $\beta$ -coupling

$\beta < \sim 0.2$



$\lambda = \text{Log}(\Lambda/\text{GeV})$

notice that this extra degree of freedom is almost unexploited

At 1 sigma,  $\beta < 0.2$   
but, at 2-sigma's, little restrictions



# Structure formation

## PS formalism

Press & Schechter 1974, ApJ 187

Improved by

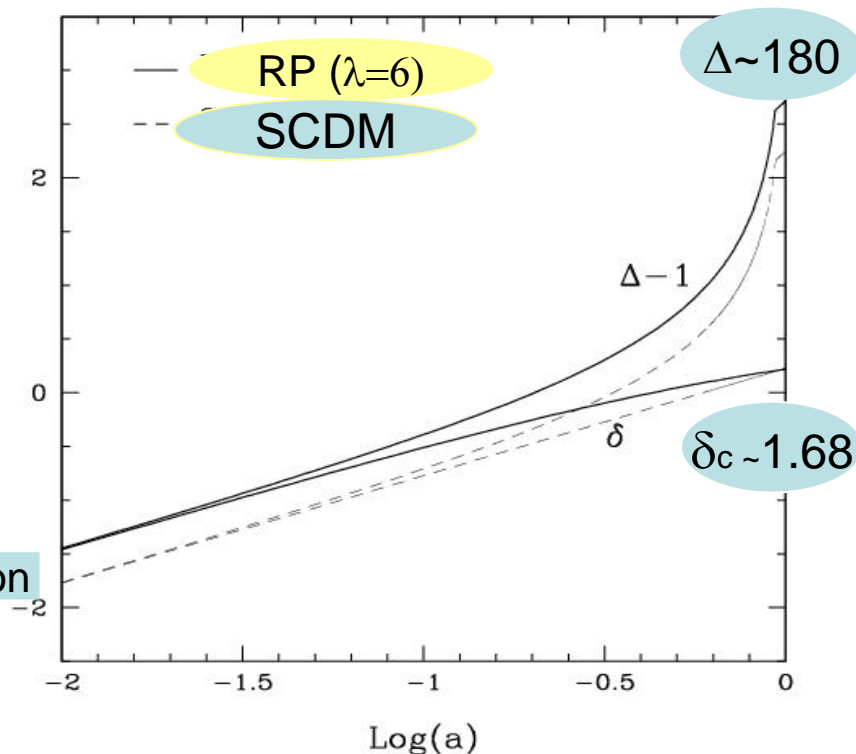
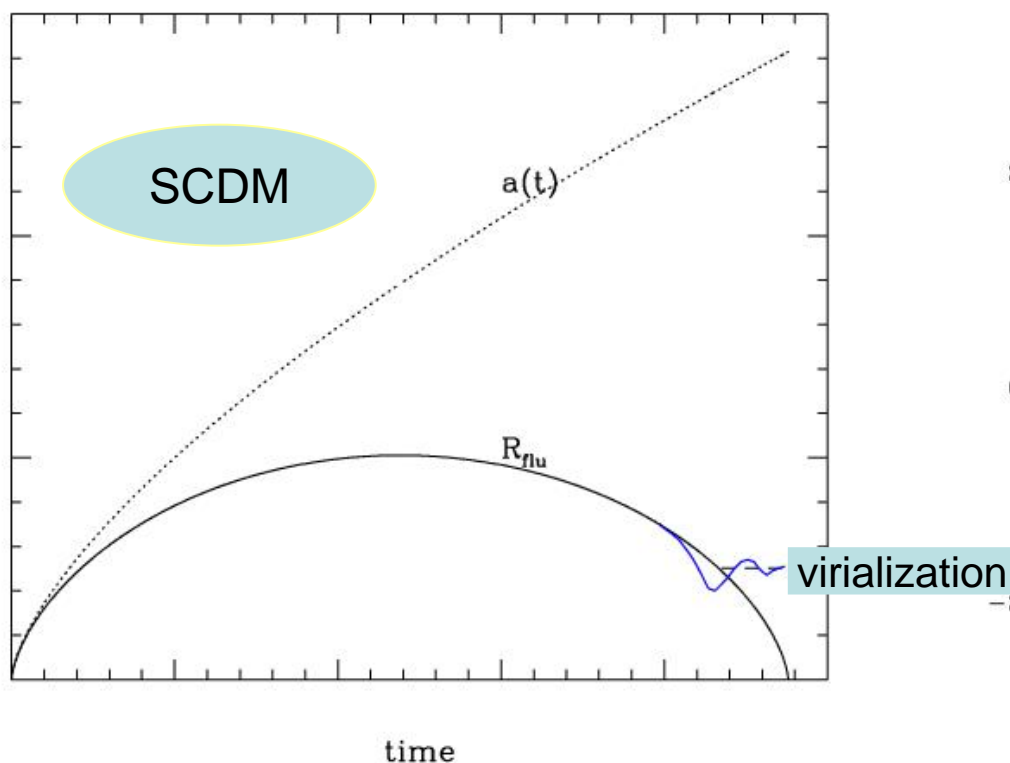
Sheth & Tormen 1999, MNRAS; Jenkins et al., 2001, MNRAS 321

allows  
to find which  
linear  $\delta_c$  would  
have fluctuations  
virializing today

Starting point: spherical top-hat fluctuation growth

Fluct. radius ( $R_{\text{flu}}$ ) expands and recontracts while the scale factor  $a(t)$  drives cosmic exp.

non-linear density contrast growing more fastly than linear fluctuation



# The PS expression

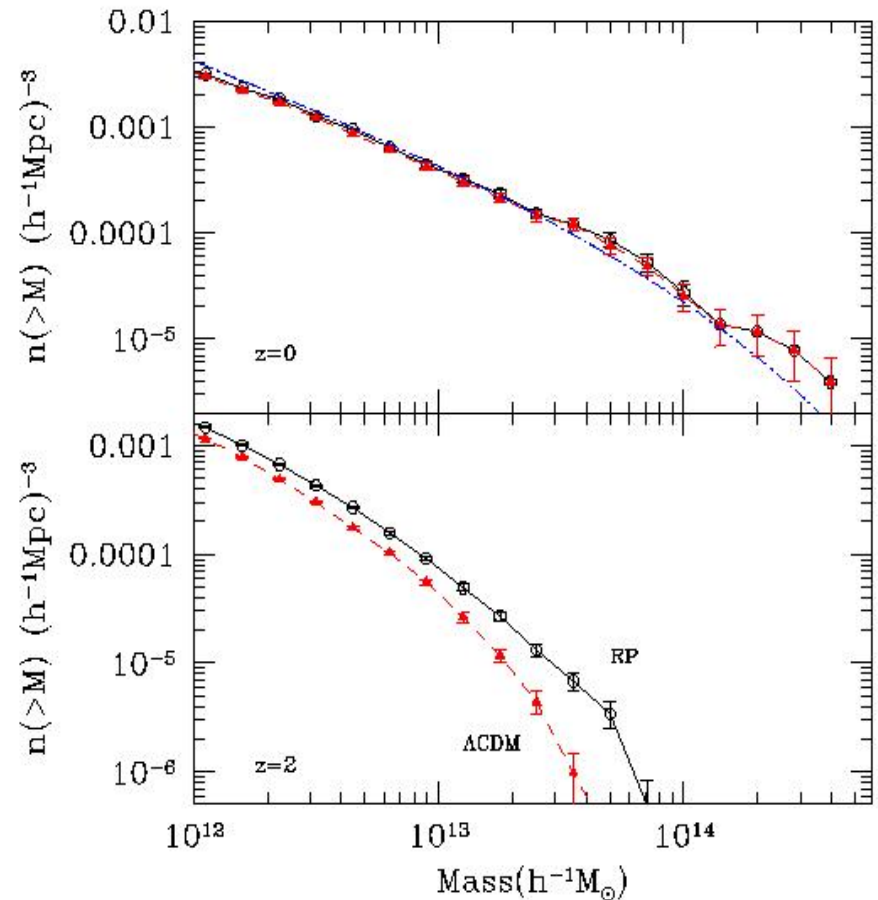
$$n(M)M dM \cong \rho_m [P(> \delta_c, M) - P(> \delta_c, M + dM)]$$

$$P(\delta) = (2\pi)^{-1/2} \int_{\delta_c / \sigma_M}^{\infty} dx e^{-x^2/2}$$

$$\frac{dP}{dM}(> \delta_c, M) = \frac{\delta_c}{\sigma_M^2} \frac{d\sigma_M}{dM} e^{-\frac{1}{2}(\frac{\delta_c}{\sigma_M})^2}$$

$$n(> M) = \frac{\rho_m}{M} \int_M^{\infty} dM' \frac{\delta_c}{\sigma_{M'}^2} \frac{d\sigma_{M'}}{dM'} e^{-(\delta_c / \sigma_{M'})^2 / 2}$$

PS is a fair  
fit to simulations  
ST takes partially into account  
non-sphericity in real fluct.  
growth, and provides  
even better  
fits



ST vs simulations

ST: dashed blue line

error bars: poisson noise

From Klypin, Maccio', Mainini & B.  
2003, ApJ 599 (dDE simulations)

## PS formulation for cDE

Based on a newtonian description of DM-DE interactions

(i) DM particle masses to vary :

$$M_c(\tau) = M_c(\tau_i) \exp[-C(\phi - \phi_i)].$$

(ii) Gravitational constant between DM particles :  $G^* = \gamma G$ .

$$C = \sqrt{16\pi G/3} \beta, \quad \gamma = 1 + 4\beta^2/3$$

*(Maccio' et al. , 2004, P.R.D 69)*

Valid  
well below  
horizon &  
for negligible  
radiative  
comp.

The  $\Phi$ -field carries a long-range interaction which appears as a correction to newtonian gravity, but only for DM-DM interactions  
B-DM interactions untouched

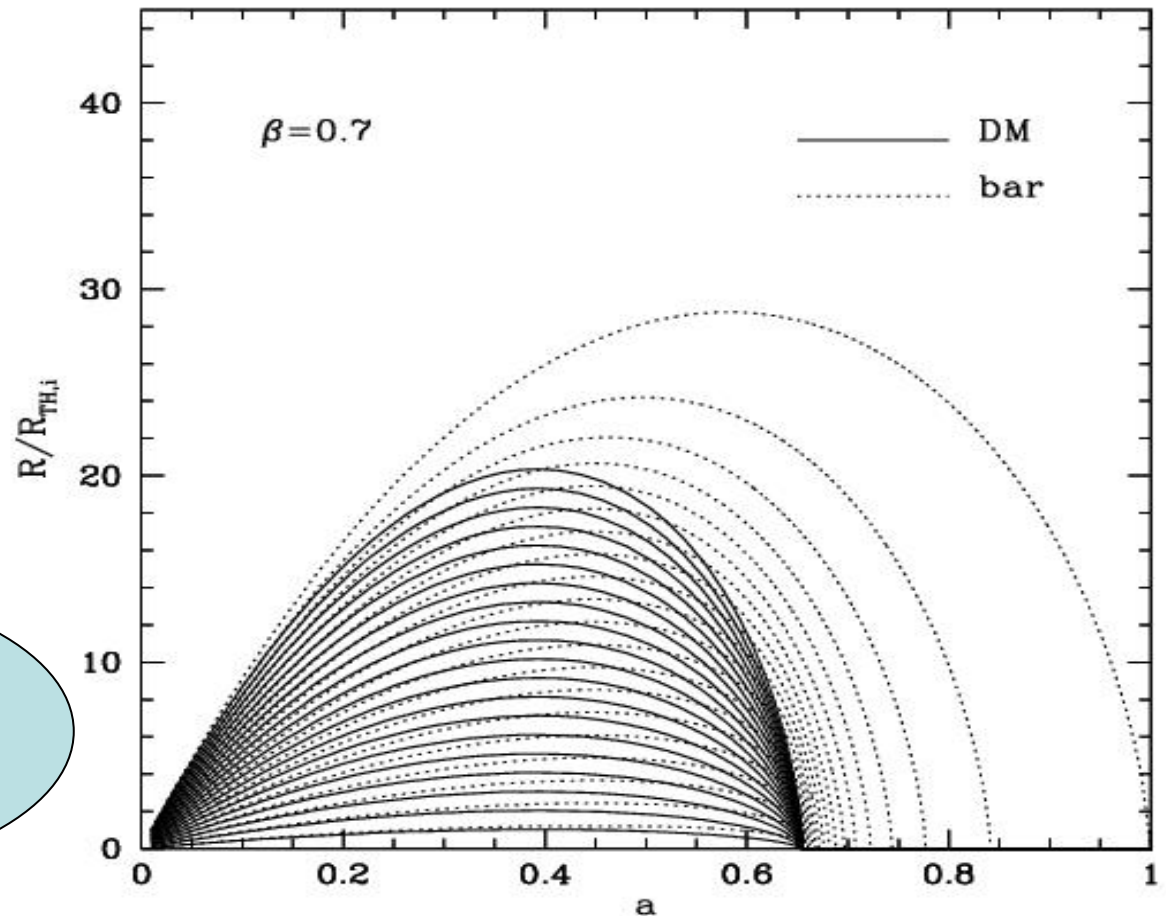


Model with  
 $\beta = 0.7$   
from Mainini, 2005, P.R.D 72

Effective  
DM gravity  
is stronger

DM shells  
evolve  
more rapidly

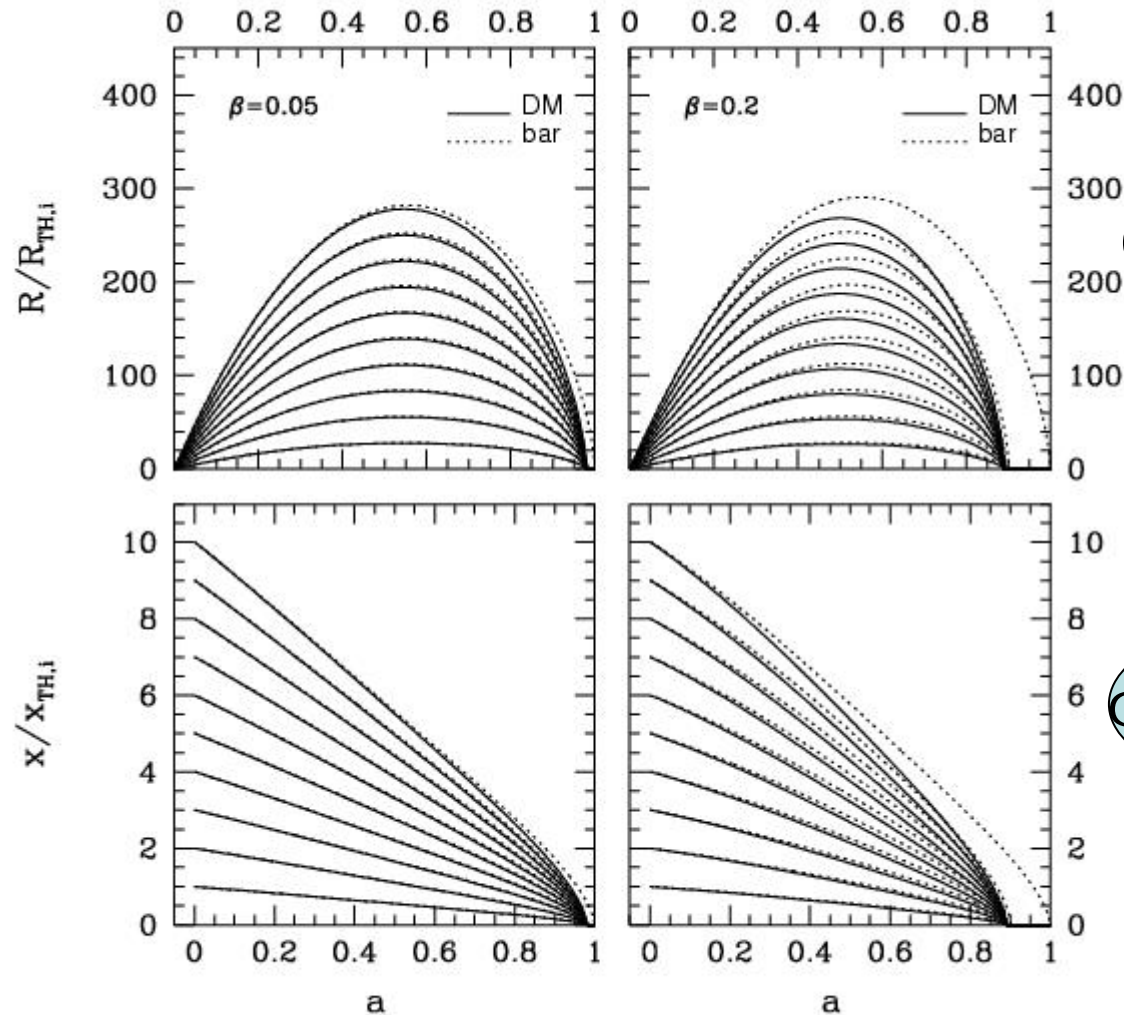
A sampling  
of spherical shells  
(~1000 used)



# Shell radii (bar & DM)

## Models of this paper

Mainini & Bonometto, PRD 2006



physical

Our model's parameters

$$\Omega_m=0.25$$

$$\Omega_b=0.042$$

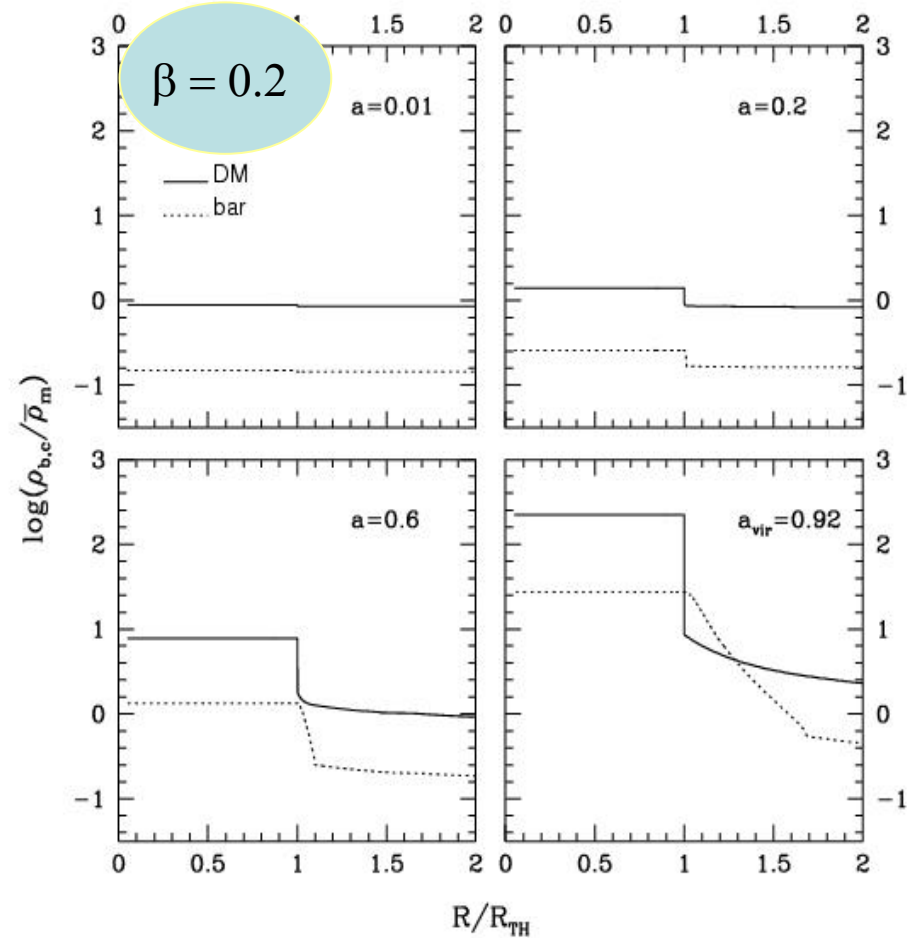
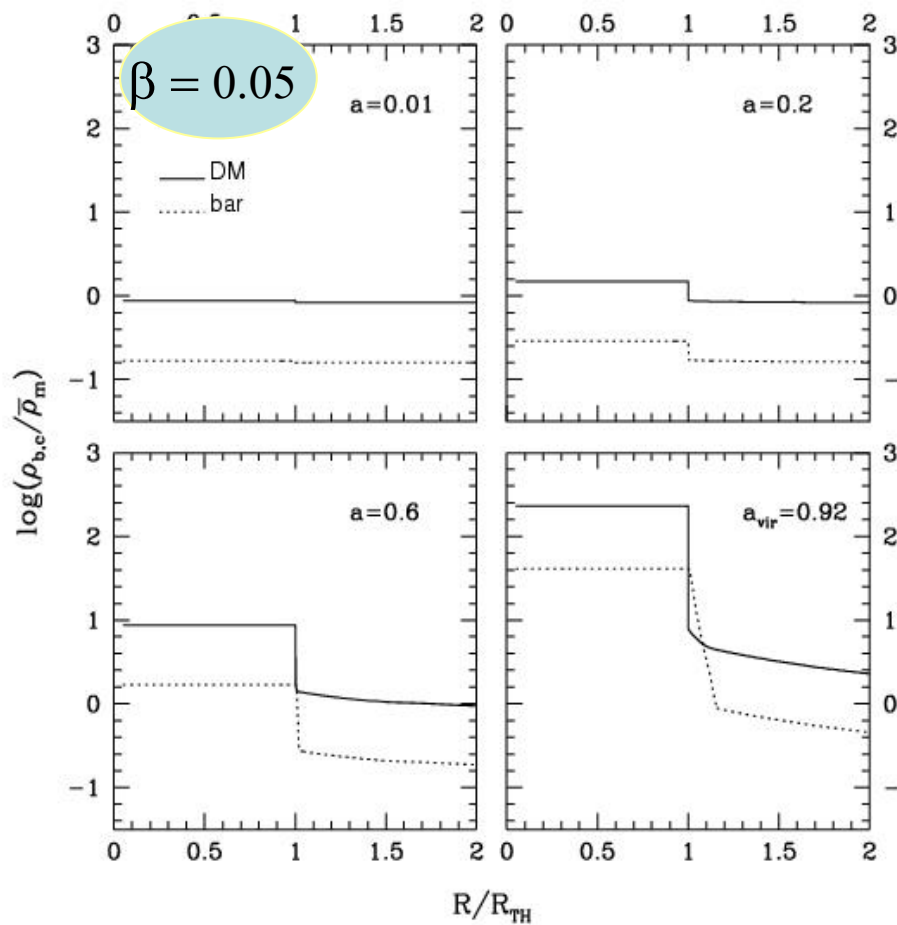
$$h=0.73$$

WMAP1

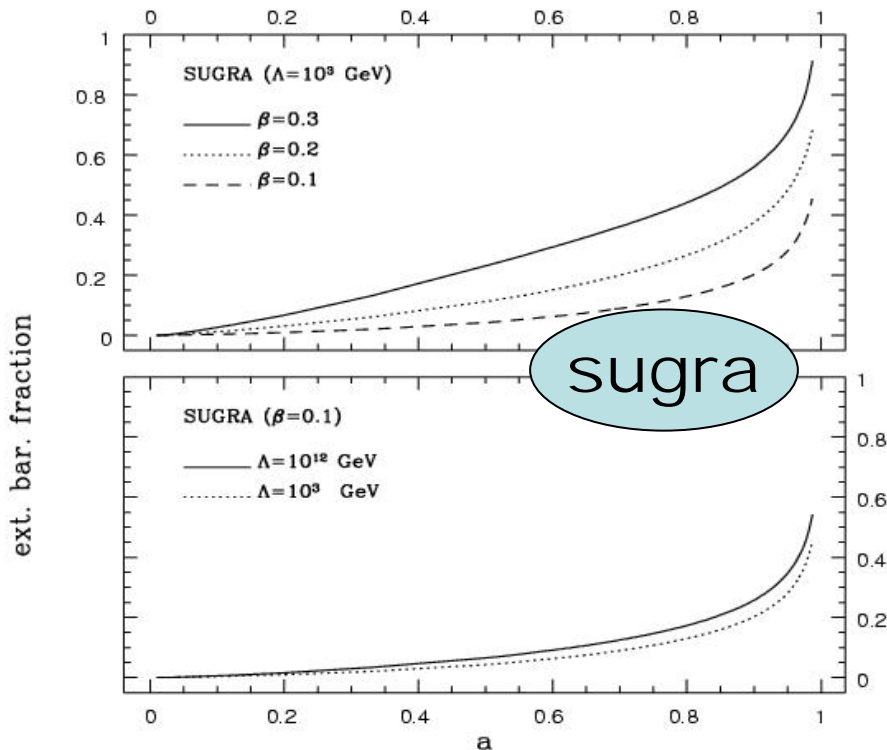
comoving

# Profile evolution, in bar. & DM until virialization

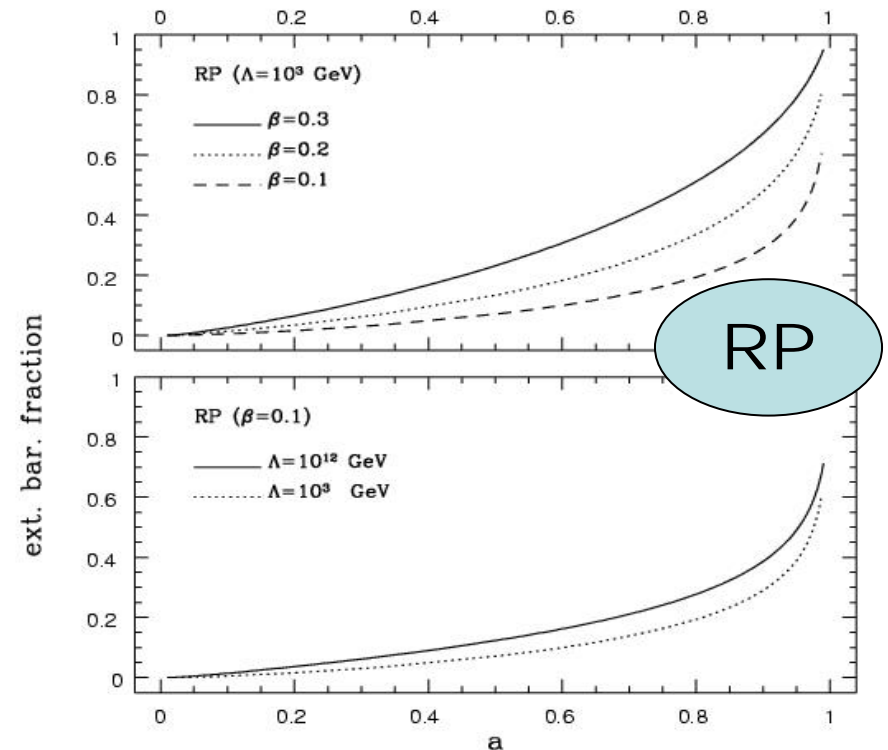
How small  
can be  $\beta$ , to yield  
appreciable  
shifts ?



# Baryon fraction leaking DM bulk



fraction increases  
with  $\beta$   
almost independent  
from  $\Lambda$

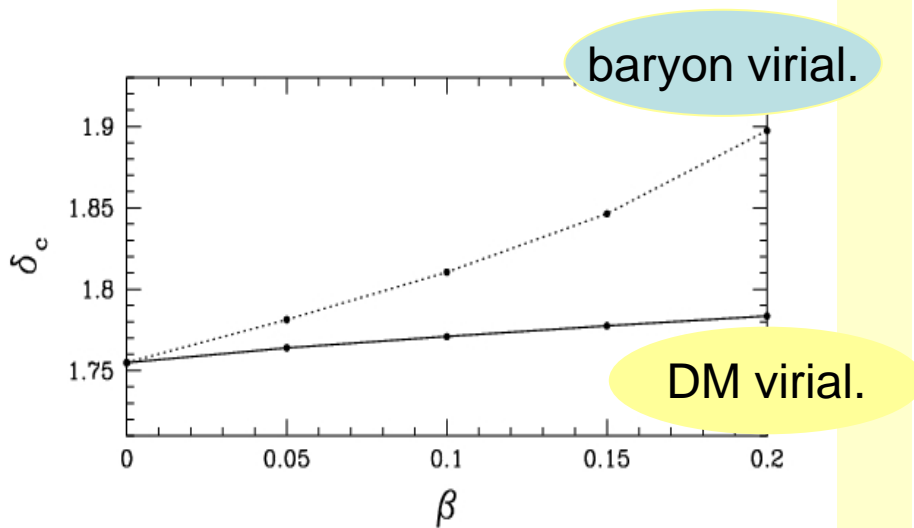


RP fraction greater

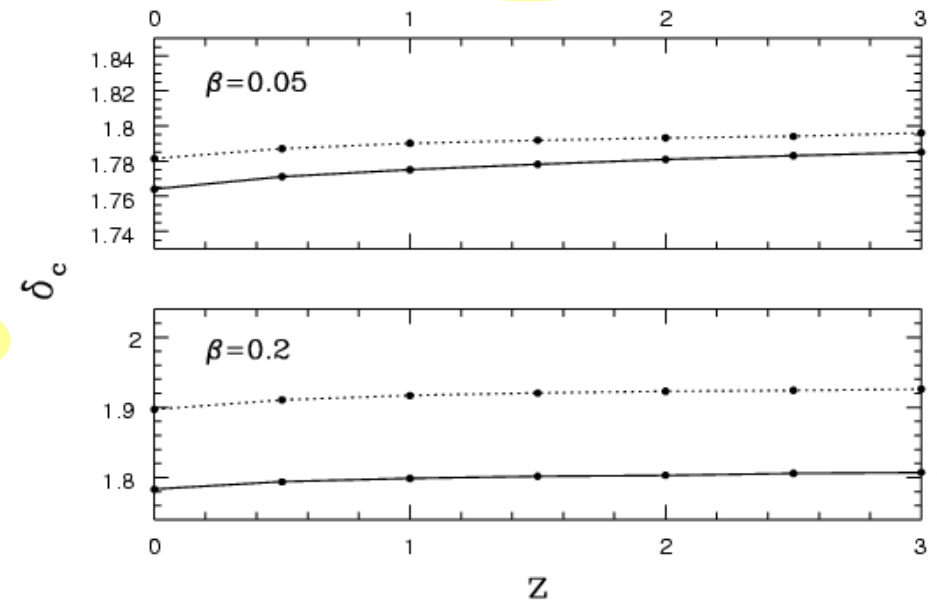
Linear amplitudes (SUGRA)

to be used in PS or ST expressions

2 different  
values for  $\delta_c$   
fluct. ampl  $\rightarrow$  DM virial.  
Fluct.ampl  $\rightarrow$   
baryon virial.

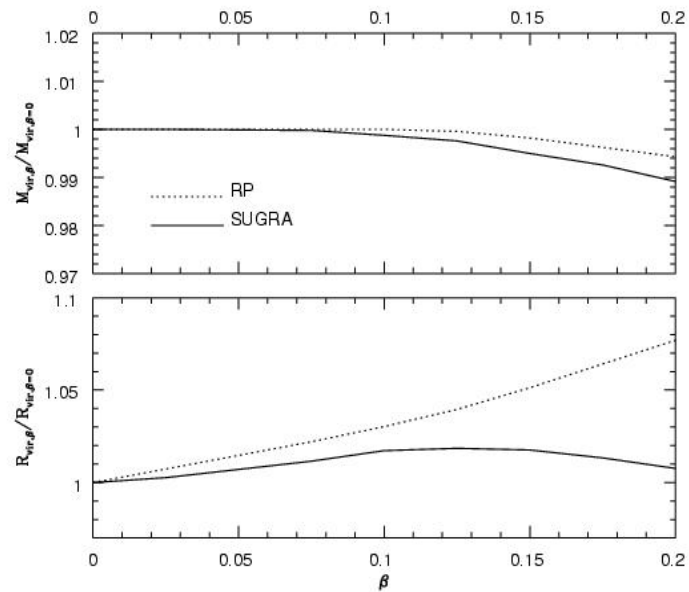


$\beta$  dependence at  $z=0$

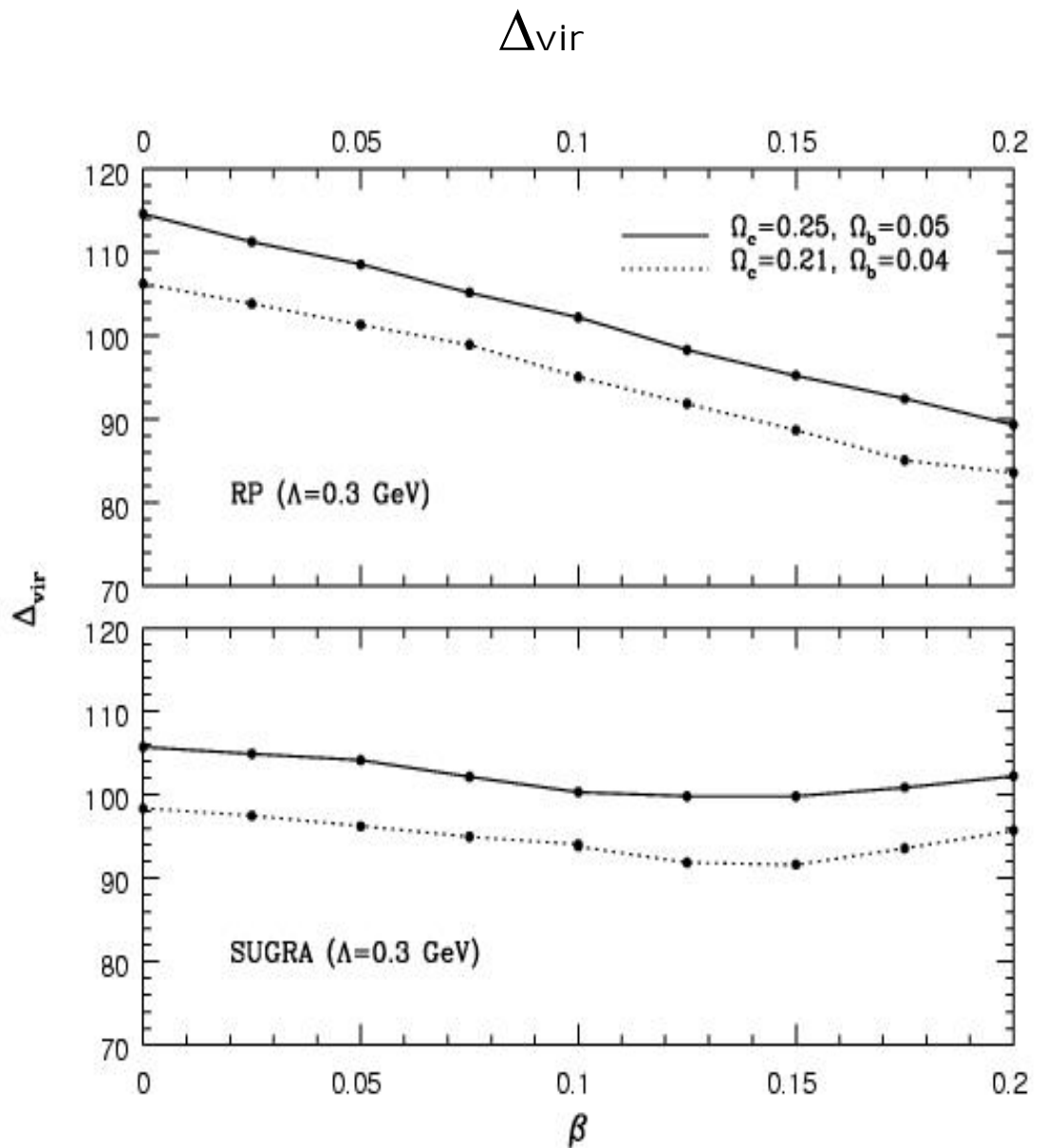


$z$  dependence for model's  $\beta$

$M_{\text{vir}}$  &  $R_{\text{vir}}$  vary  
because of coupling



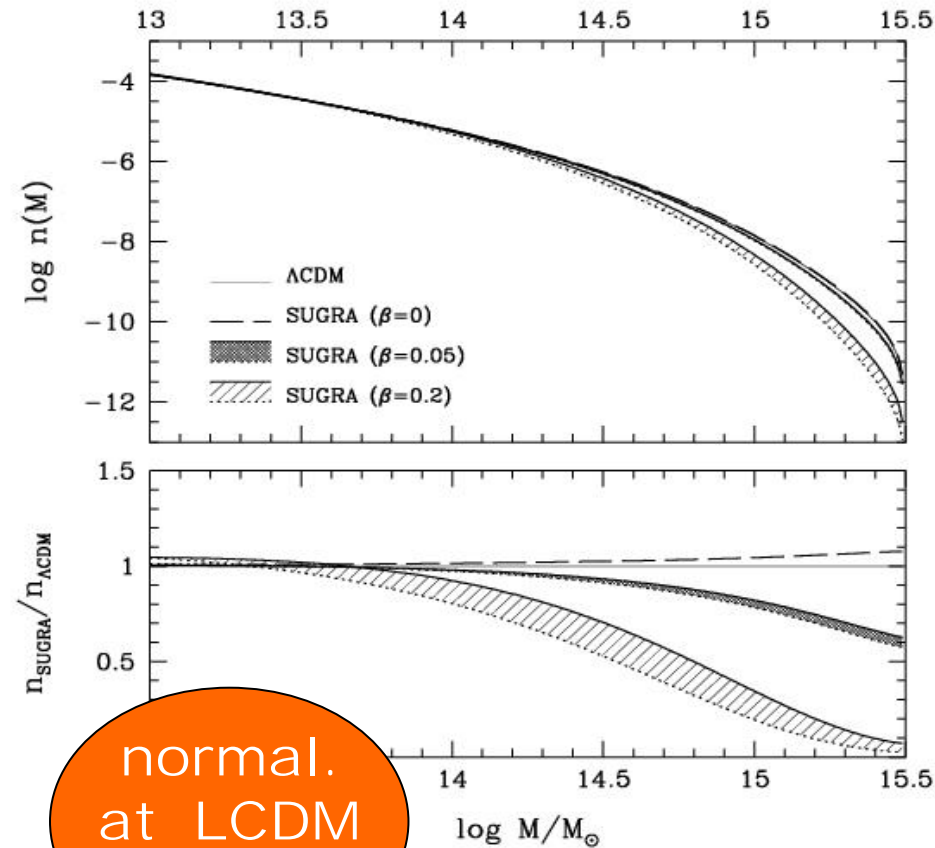
to be  
used to find  
halos in  
simul.



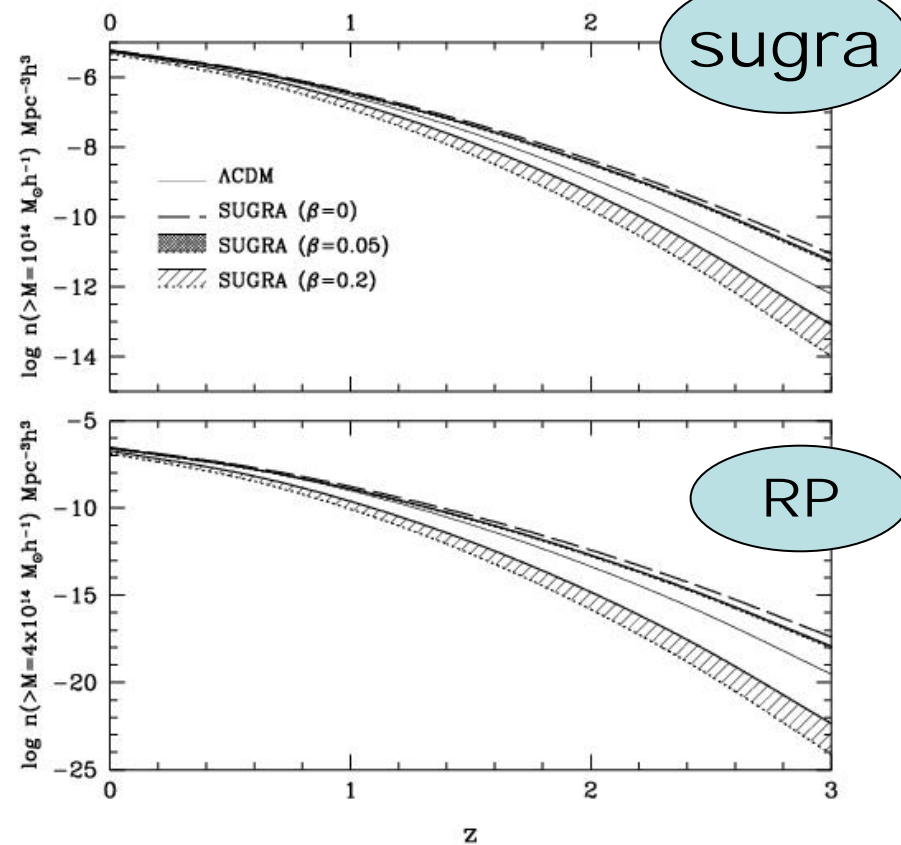


# PS mass functions at $z=0$

N vs redshift  
in comoving volumes



normal.  
at LCDM  
values



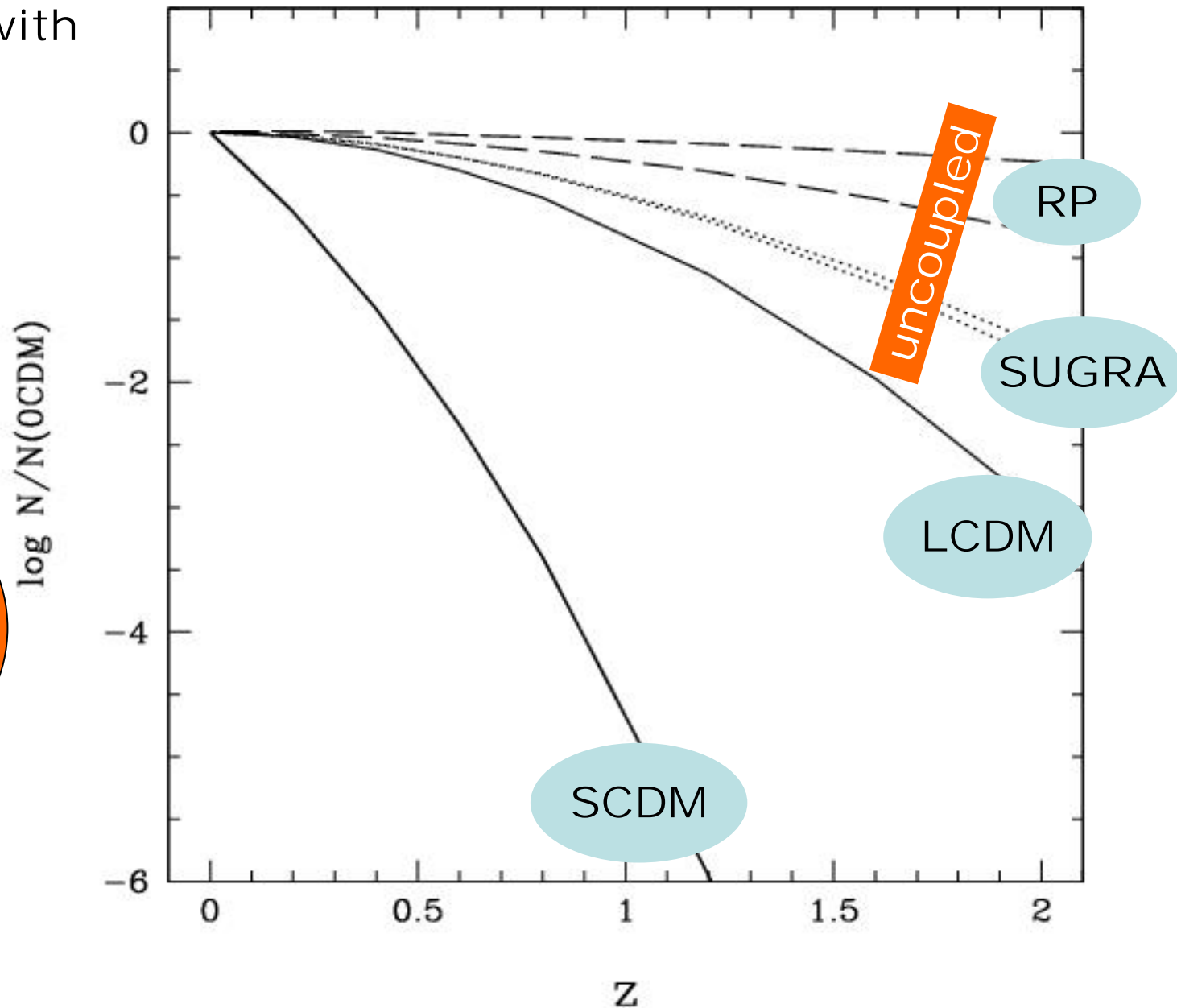
sugra

RP

signal of coupling at  $z=0$ ,  
expected if  $\beta \sim 0.2$

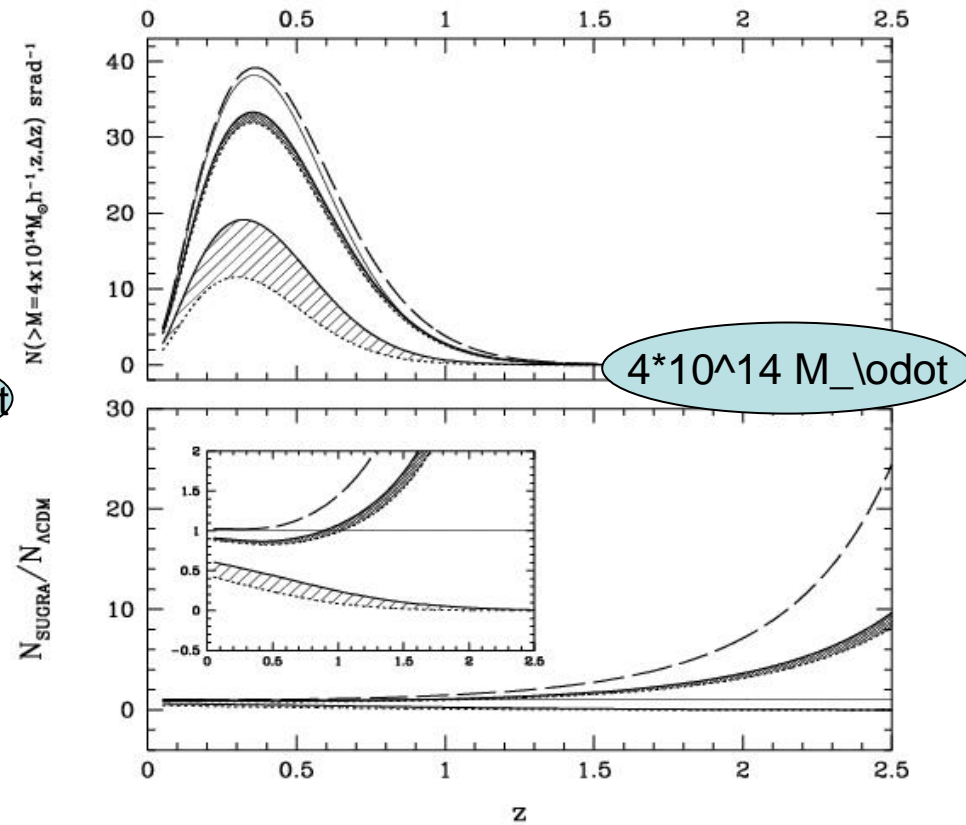
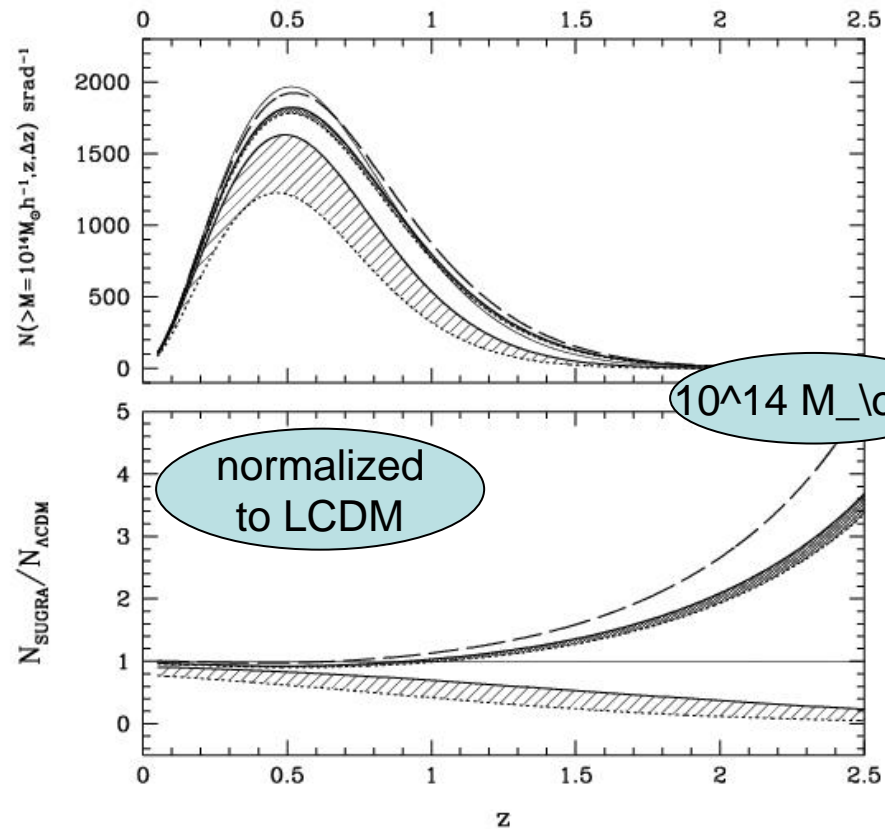
halo # evolution  
compared with  
 $\Lambda$ CDM

plots  
 $M = 5.6 \cdot 10^{14}$   
 $h^{-1} M_{\text{sun}}$





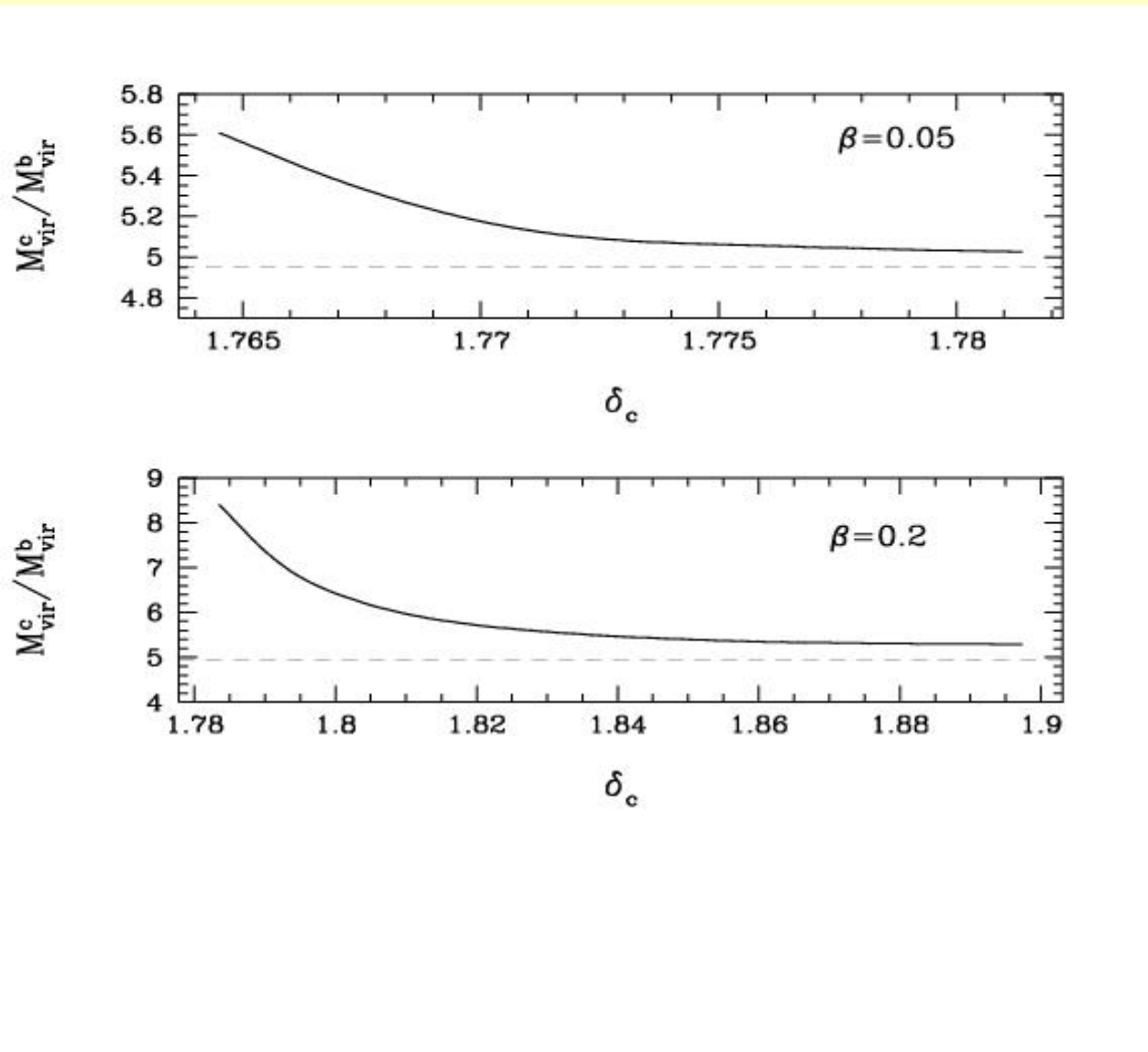
# # of expected halos in fixed $\Delta z$ and solid angle



dDE evolves  
more slowly than  
LCDM

coupling can invert  
dDE displacement

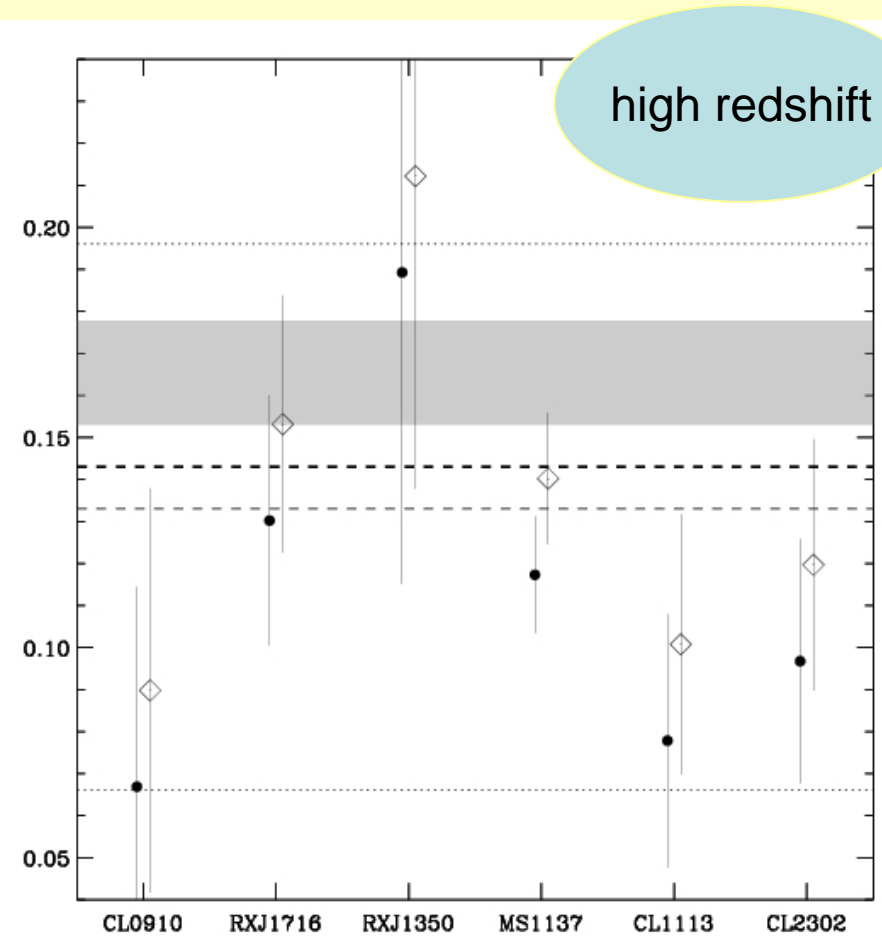
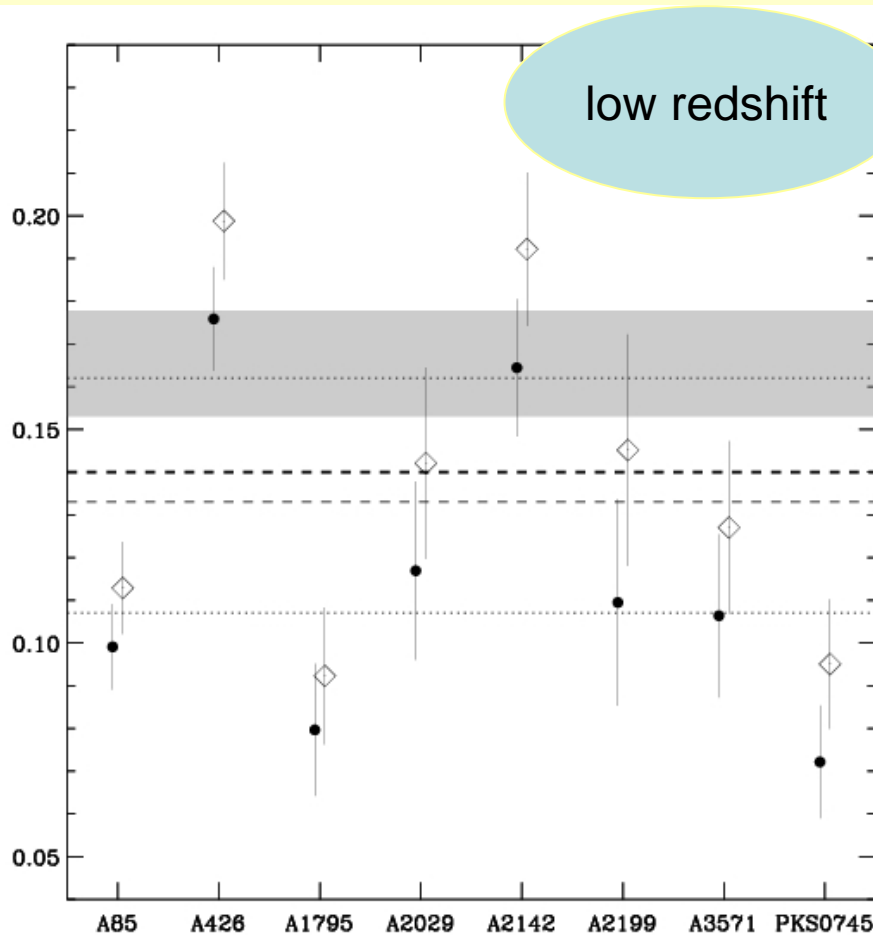
Halos are however baryon impoverished



# Baryons in galaxy clusters

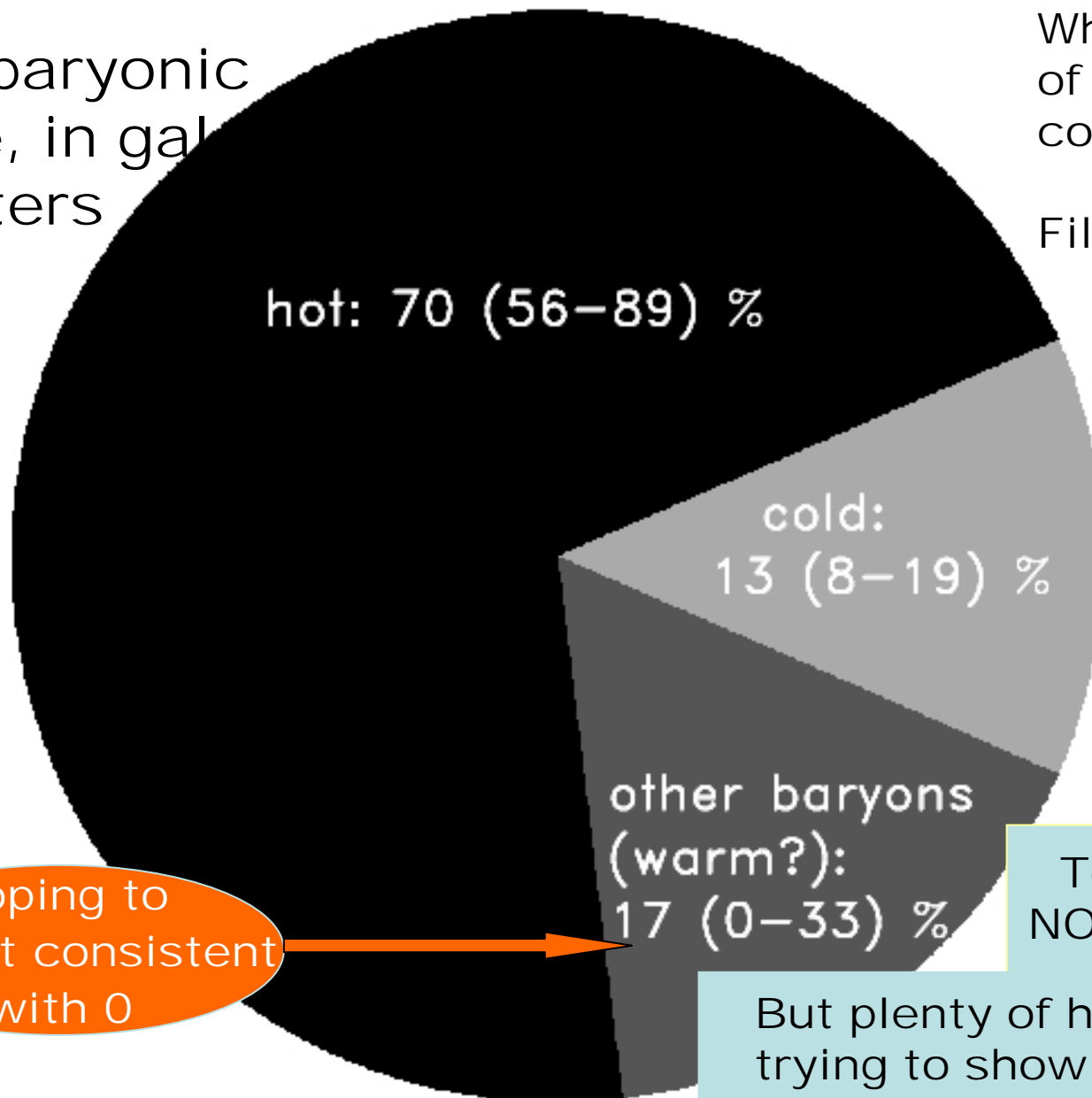
Ettori, 2003, MNRAS 344

grey band: WMAP1 data interval



black dots: intracluster gas emitting X-rays  
diamonds: total baryon budget

The baryonic  
cake, in gal  
clusters



Which evidence  
of the warm  
component ?

Filaments emitting:

Soft x-rays :  
Kaastra et al.,2003,  
A&A397  
Finoguenov, Briel  
& Henry,2003,A&A410

UV :  
Mittaz, Lieu & Lockman,  
1998, ApJL 498  
Maloney & Bland-  
Howthorn, 2001, ApJL  
553

hoping to  
make it consistent  
with 0

To my knowledge  
NO more recent data

But plenty of hydro simulations  
trying to show that:

- Warm phase forms
- Baryons expelled by early SNe



cDM simulation  
 $\Omega_m = 0.3$   
 $\Omega_b = 0.026$   
 $H = 70 \text{ km/s/Mpc}$

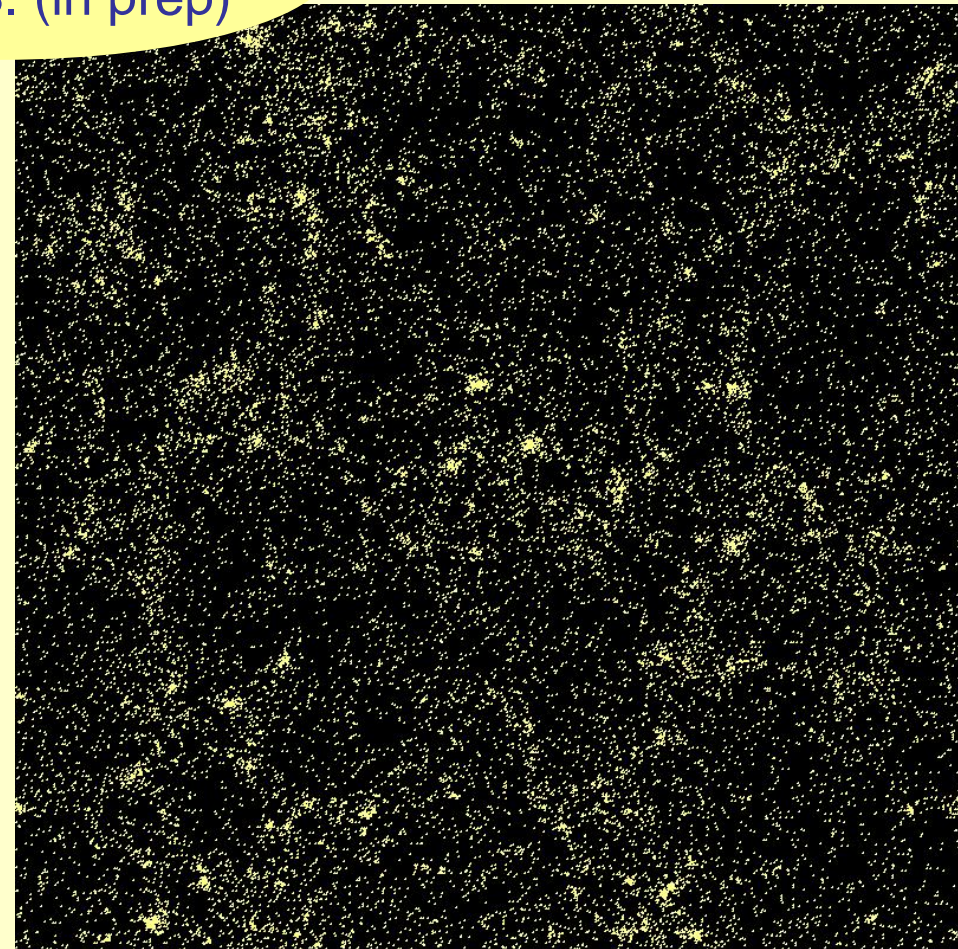
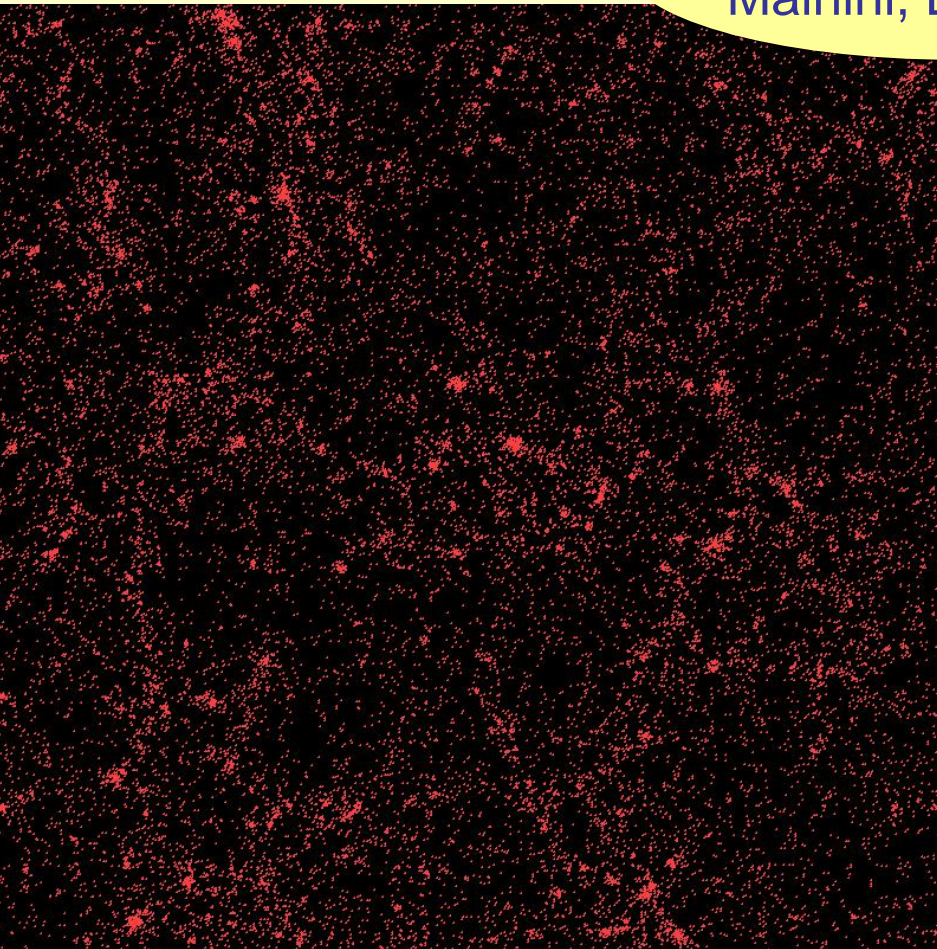
SUGRA potential  
 $\Lambda = 100 \text{ GeV}$   
 $\beta = 0.16$

ART program modified  
Box: 90 Mpc  
 $64^3 \text{ part./8 ref.lev.}$

dm

Maccio', Casarini,  
Mainini, B. (in prep)

bar



Former simulation performed in 2004  
with RP potential

Maccio', Quercellini, Mainini, Amendola, B., 2004, P.R.D69

Principal findings: limits on coupling  
In RP models the  $\phi$  field is always increasing  
Corrections to DM gravity stronger in the past  
→ highly concentrated halos

Only for  $\beta < 0.2$  concentration acceptable

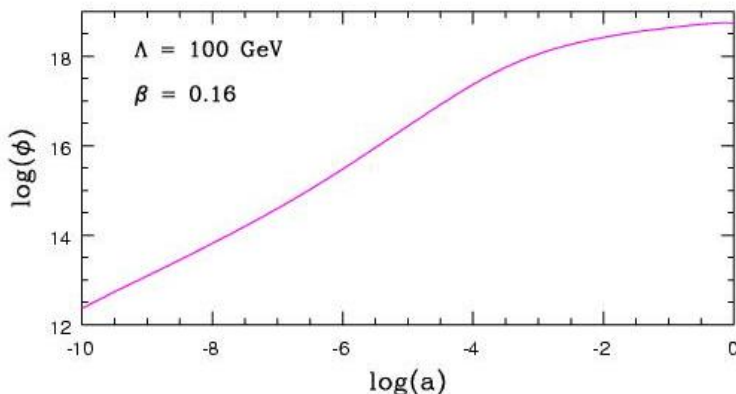
NO test on baryon depletion made on it

RP potential

$$V(\phi) = \Lambda^{4+\alpha} / \phi^{\alpha}$$

Main difficulty with ART  
implementation: agreement  
btwn finite step length and  
continuous M and G variat.

An easy  
solution for monotonic  
field variation



With SUGRA potential,  $\phi$  increase stopped  
by exp factor; with selected parameters,  
the recent  $\phi$  behavior almost flat  
Halo concentration no longer a problem



Box contains

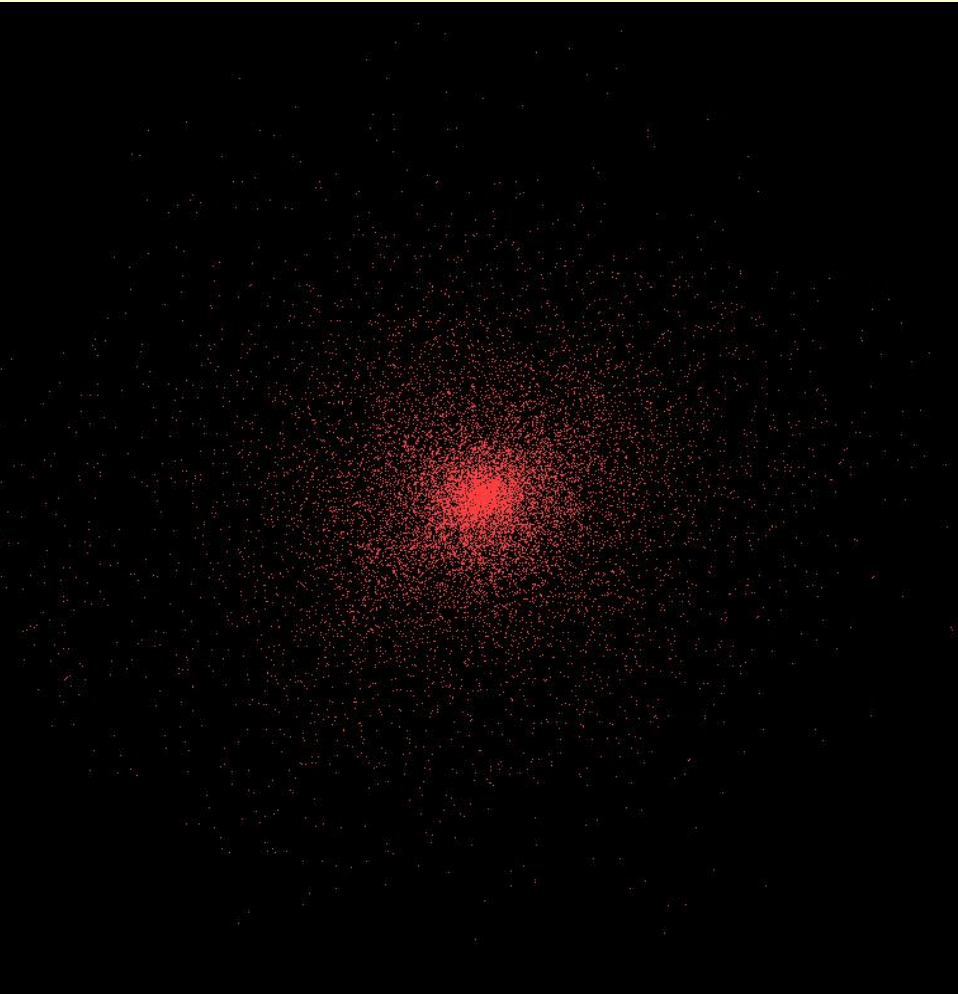
153 halos in mass interval:  
 $2.3 \times 10^{13} M_{\odot}$  (100 part) -  
 $2.5 \times 10^{14} M_{\odot}$  (1089 part)

8 halos magnified

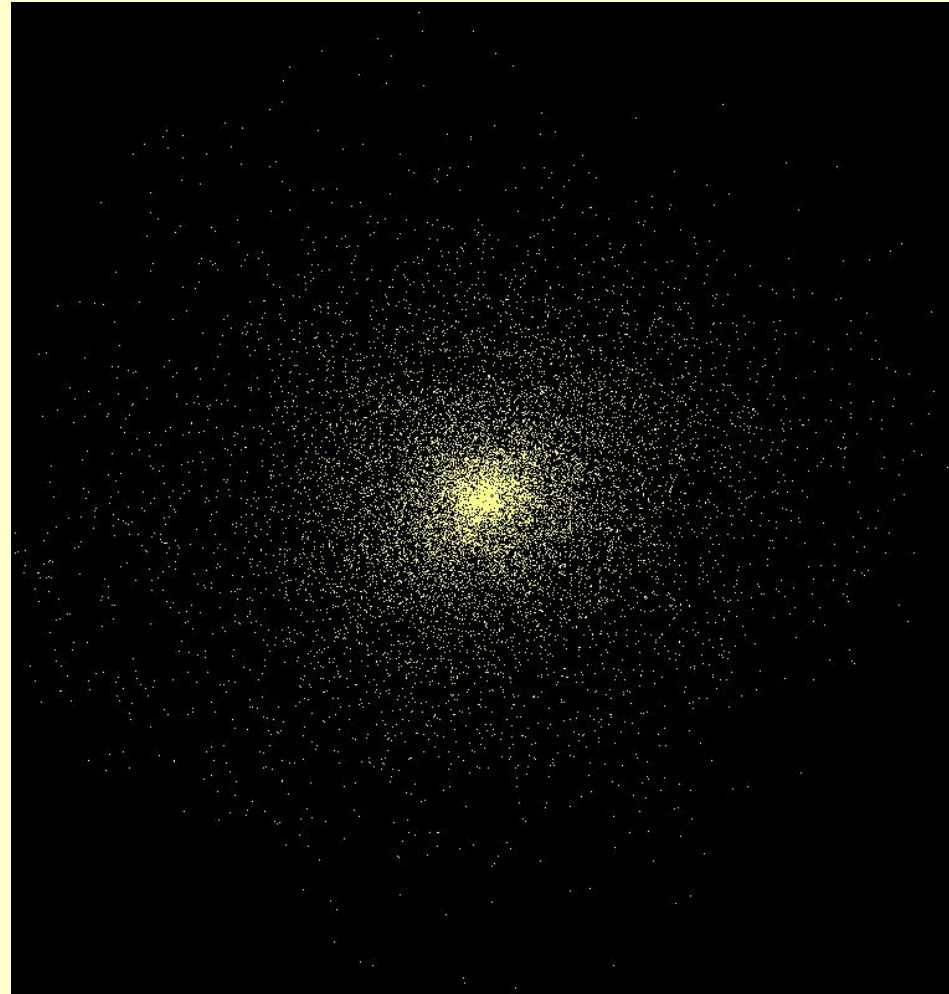
8 levels in mass

5 levels in force

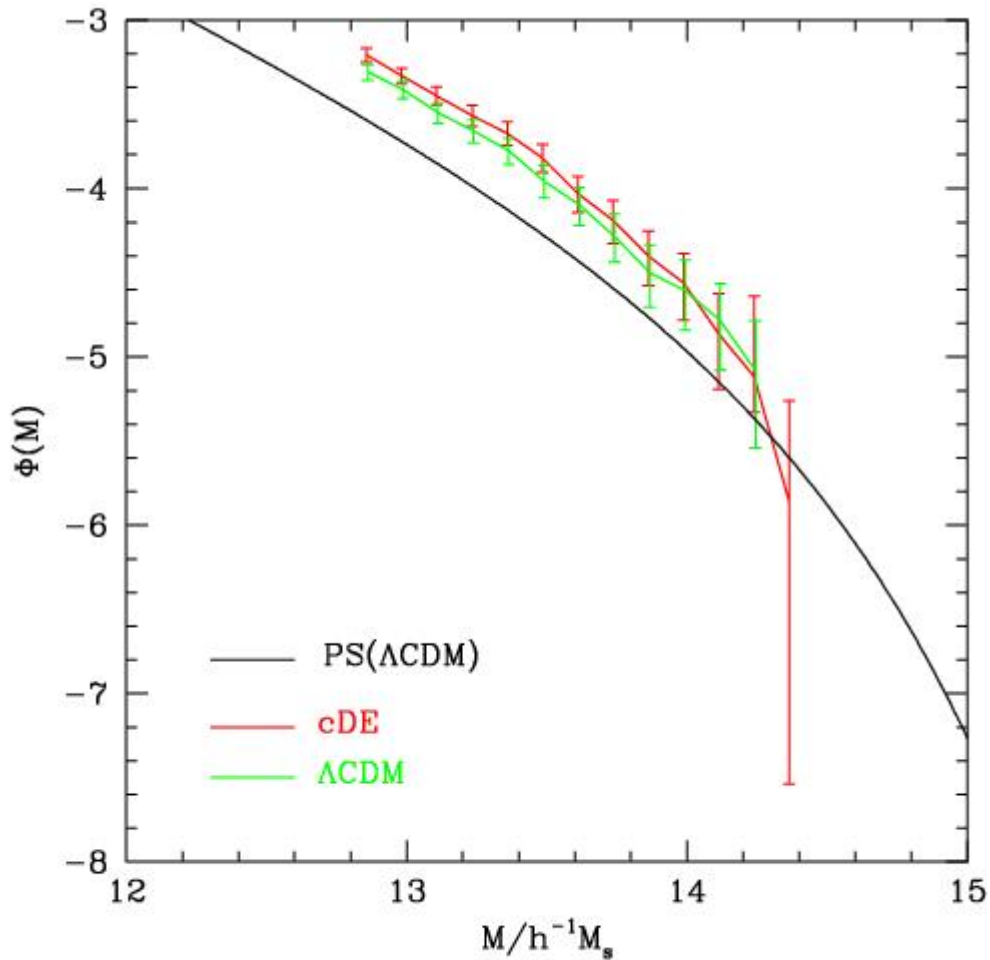
dm



bar



## Mass function



Same  $\sigma_8$   
for coupled SUGRA  
and LCDM

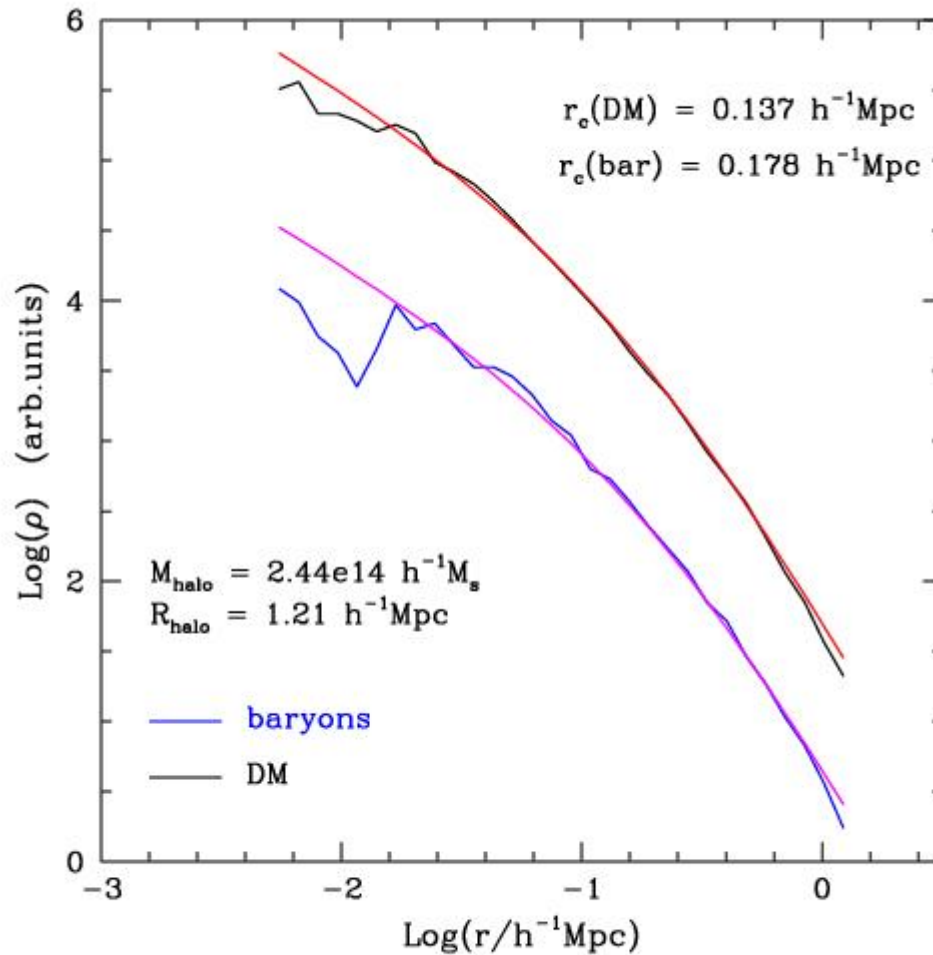
369 halos in LCDM  
470 halos in cDE

>30 particle halos

Mild disagreement with PS  
ST fits better



# Halo profile for DM and baryons, NFW fits



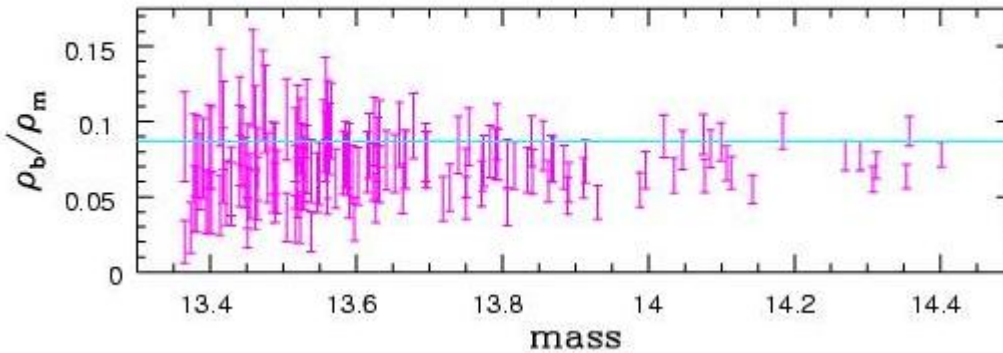
Different concentrations for DM & bar.

# baryon depletion

Blue line is the background abundance

All halos

Error bars are poisson noise



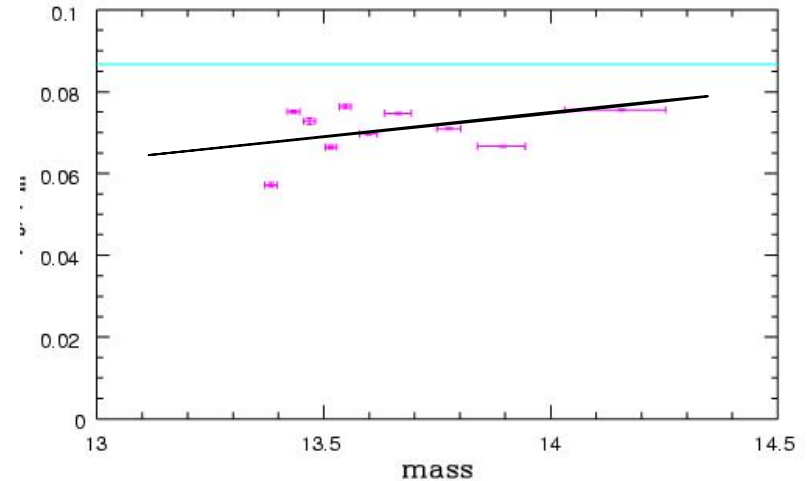
average depletion ~17 %

(all halos with >31 particles)

Sets of 15 halos

Error bars are 1- $\sigma$  standard deviation

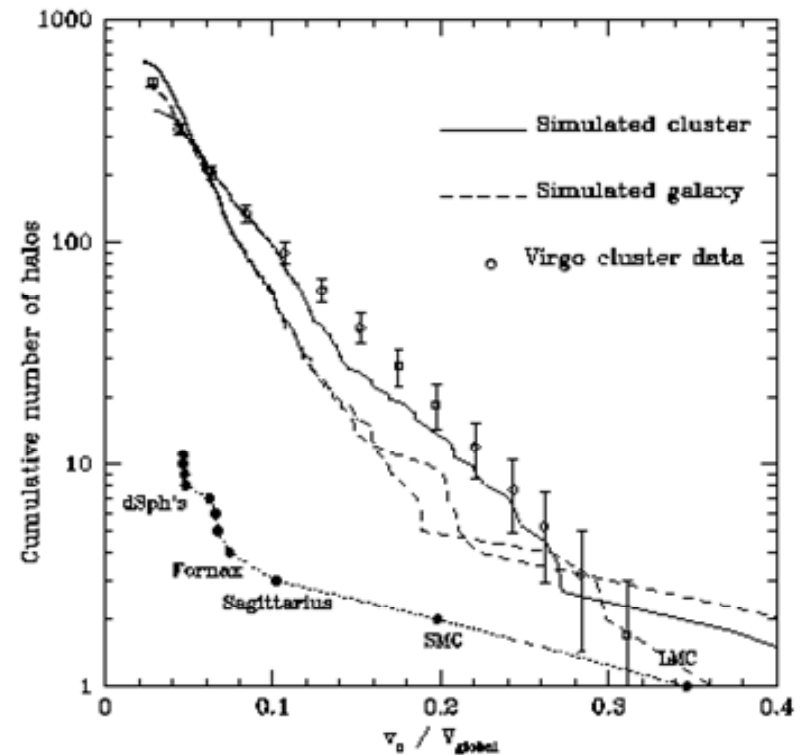
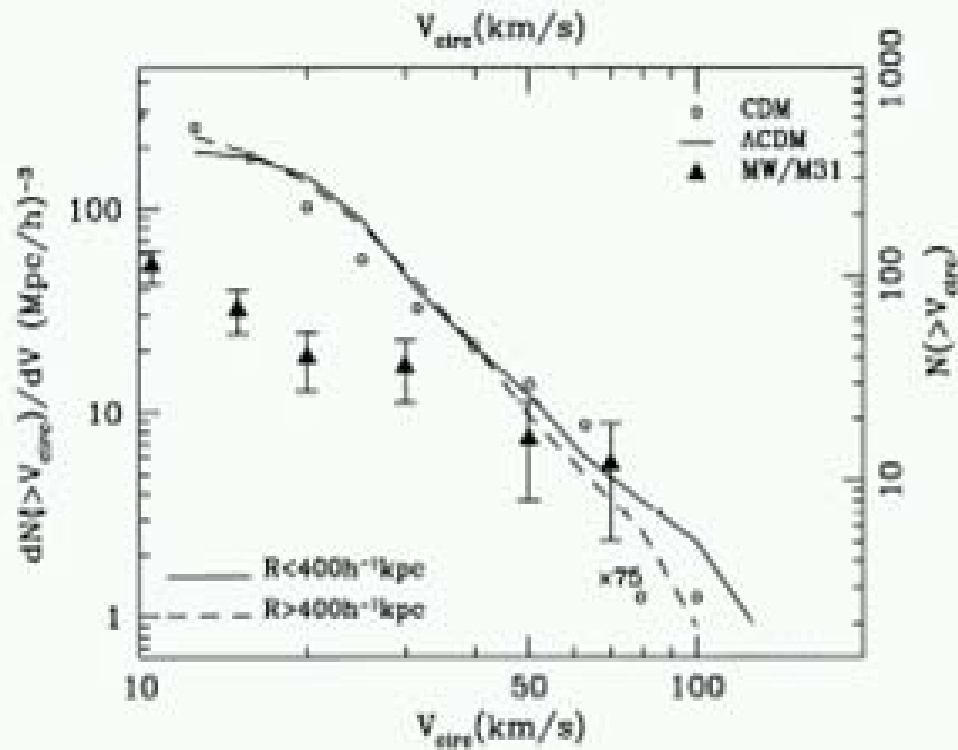
Only halos with >100 particles



A trend  
in baryon  
depletion ?

ANDROMEDA  
SATELLITES





Klypin et al., 1999, ApJ 522

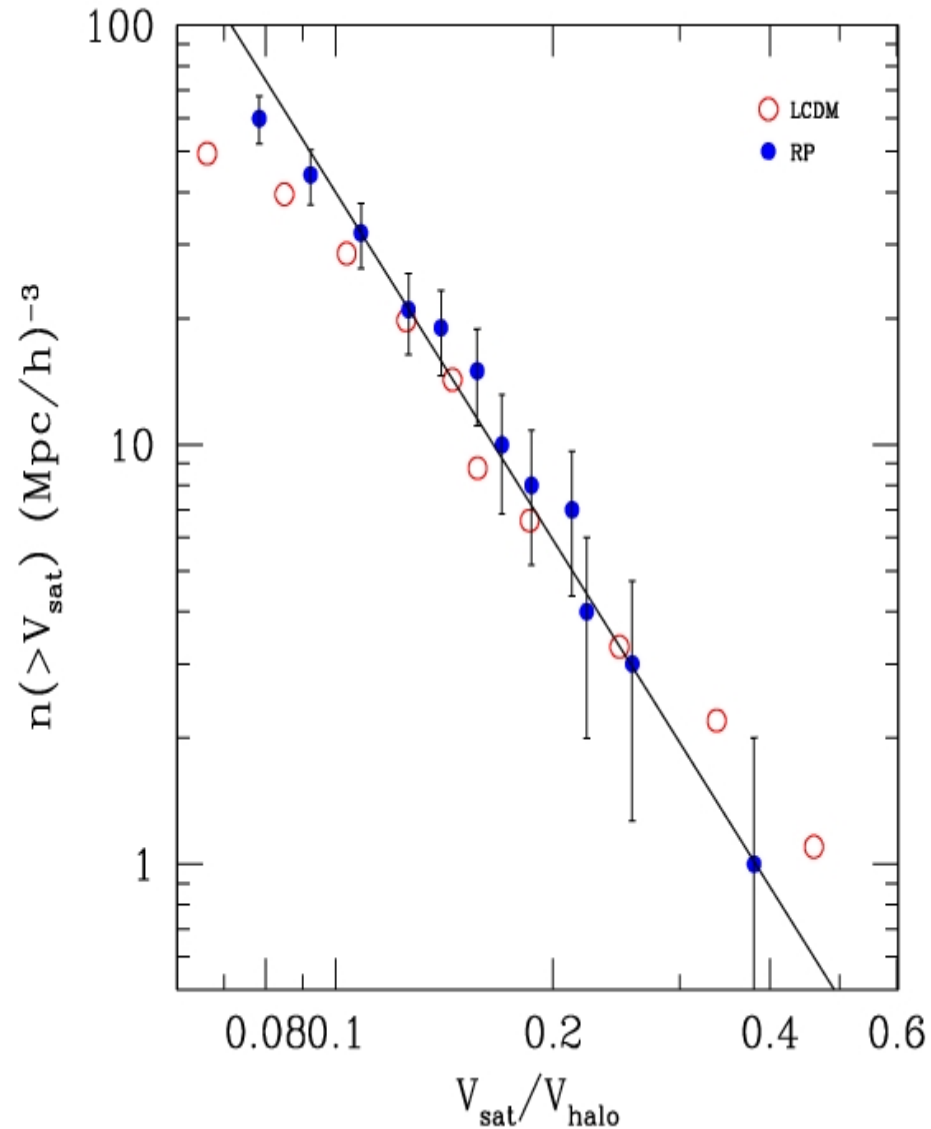
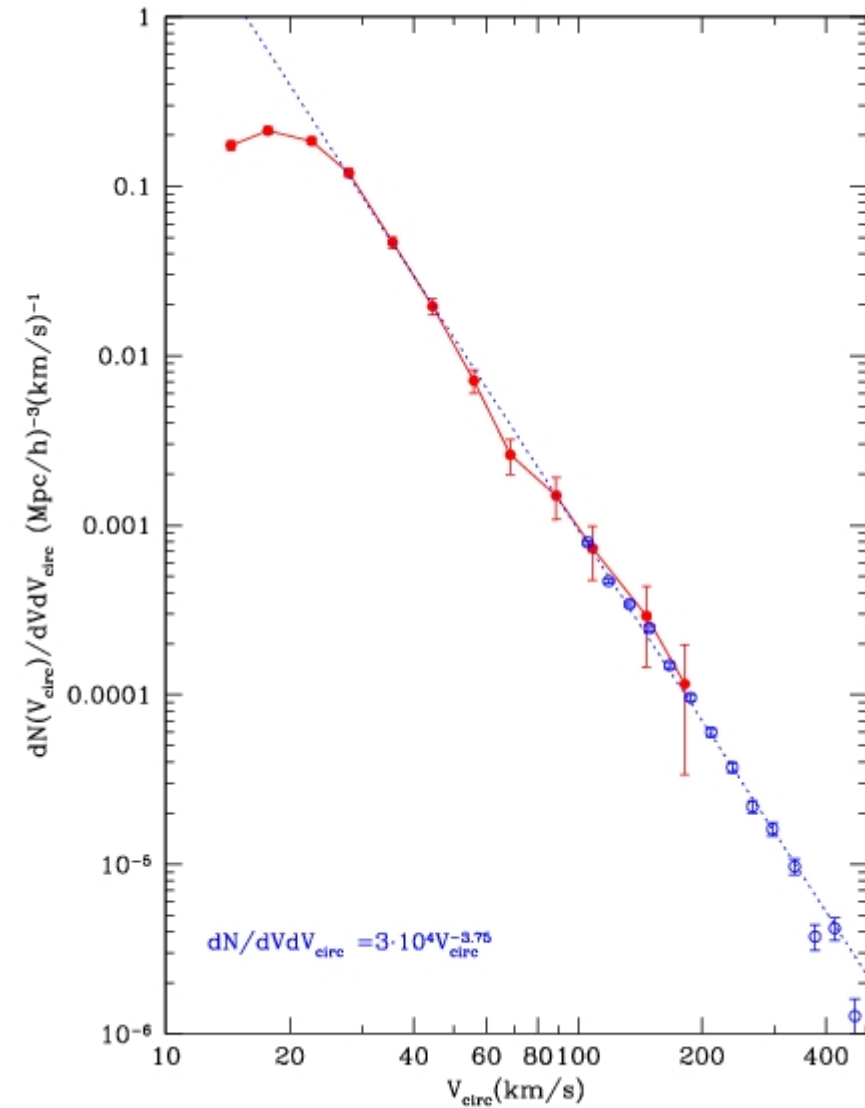
Where are the  
missing galaxy  
satellites ?

Moore et al., 1999, ApJ 524

Metcalf & Madau,  
2001, ApJ 563

2 solution: missing satellites did not form  
missing satellites are there, but invisible...

# DARK SATELLITES



Klypin, Kravtsov, Valenzuela & Prada, 1999, ApJ 522  
see also Moore et al, 1999, ApJL 524

dDE, # of satellites predicted  
the same as for LCDM  
Klypin et al, 2003, ApJ 599

# CONCLUSIONS

DM+LAMBDA models  
are an excellent 'caloric' description  
of the Dark Substance, but...

N-body simulations of cDE cosmologies  
yield promising results  
with fairly acceptable coupling strengths

already  
 $\beta \sim 0.05$   
yields fair  
effects

In the sensitive areas  
a number of data require different dynamics  
for DM & baryons; here we considered  
baryon depletion in clusters

Similar patterns to be explored  
whenever hydrodynamics does not provide  
bar-DM segregation mechanism acting early enough  
In turn, this can provide rich information  
on DM-DE relations